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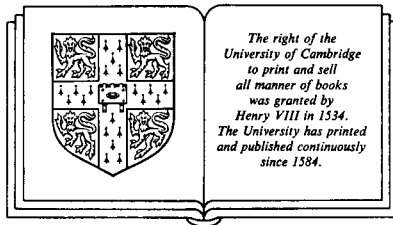
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CAMBRIDGE UNIVERSITY PRESS
Cambridge
New York New Rochelle Melbourne Sydney

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CAMBRIDGE UNIVERSITY PRESS
Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo, Delhi

Cambridge University Press
The Edinburgh Building, Cambridge CB2 8RU, UK

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org
Information on this title: www.cambridge.org/9780521265935

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First published 1987
This digitally printed version 2008

A catalogue record for this publication is available from the British Library

Library of Congress Cataloguing in Publication data

Sachdev, P. L.
Nonlinear diffusive waves.
Bibliography
Includes index.
1. Nonlinear waves. I. Title.
QA927.S214 1987 531'.1133 86-18397

ISBN 978-0-521-26593-5 hardback
ISBN 978-0-521-09303-3 paperback

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Preface

I was fortunate to receive help from many. Professor Sir James Lighthill FRS provided the impetus to undertake this venture. Dr Allen Tayler helped my rather amorphous ideas assume a precise form. Professor A. Richard Seebass, many years ago, introduced me to the mysteries of Burgers' equation and its kindred class. I had the benefit of very fruitful discussions with Professors D. G. Crighton and J. D. Murray. Professor Colin Rogers read through parts of the manuscript. Professors P. N. Kaloni and M. C. Singh were excellent hosts during my sojourns at the Universities of Windsor and Calgary, where I wrote part of the book. My student, Mr K. R. C. Nair, carried out much of the computations reported in the final chapter and assisted in various other ways. Ms Thelma Stanley, with good cheer and patience, typed the manuscript and many a change I made in it. Finally, I owe a lot to my wife Rita, who cared and comforted.

I gratefully acknowledge the financial assistance provided for the preparation of the manuscript by the Curriculum Development Cell, established at the Indian Institute of Science by the Ministry of Education and Culture, Government of India.

In conclusion, I thank Dr David Tranah of Cambridge University Press, for his courtesy and thoughtful consideration during the entire course of the publication of this monograph.