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978-0-521-09095-7 - Contiguity of Probability Measures: Some Applications in Statistics

George G. Roussas

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