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978-0-521-09094-0 - Entropy, Compactness and the Approximation of Operators

Brend Carl and Irmtraud Stephani

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