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References are to section numbers; those in **bold** type indicate definitions, those in *italic* passing references

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