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978-0-521-08076-7 - Algebraic Topology-A Student's Guide  
J. F. Adams  
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# Algebraic Topology – A Student's Guide



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