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978-0-521-06674-7 - The Foundations of Differential Geometry

Oswald Veblen and J. H. C. Whitehead

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