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978-0-521-06512-2 - Bipartite Graphs and their Applications

Armen S. Asratian, Tristan M. J. Denley and Roland Haggkvist

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