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978-0-521-06508-5 - Mathematical Programs with Equilibrium Constraints

Zhi-Quan Luo, Jong-Shi Pang and Daniel Ralph

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