

## Index of Symbols

This is a list of some of our symbols – along with the pages where they are defined. A few symbols have more than one meaning.

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