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978-0-521-01107-5 - Elementary Geometry of Differentiable Curves: An Undergraduate Introduction

C. G. Gibson

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