

Transcendence Cambridge University Press PHTP 108 V42494 Table Applications of Diophantine Approximation to Integral Points and Table of Contents More Information

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