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# Surveys in Combinatorics 2017

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CAMBRIDGE  
UNIVERSITY PRESS

Cambridge University Press

978-1-108-41313-8 – Surveys in Combinatorics 2017

Edited by Anders Claesson , Mark Dukes , Sergey Kitaev , David Manlove , Kitty Meeks

Frontmatter

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CAMBRIDGE  
UNIVERSITY PRESS

University Printing House, Cambridge CB2 8BS, United Kingdom

One Liberty Plaza, 20th Floor, New York, NY 10006, USA

477 Williamstown Road, Port Melbourne, VIC 3207, Australia

4843/24, 2nd Floor, Ansari Road, Daryaganj, Delhi – 110002, India

79 Anson Road, #06-04/06, Singapore 079906

Cambridge University Press is part of the University of Cambridge.

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Information on this title: [www.cambridge.org/9781108413138](http://www.cambridge.org/9781108413138)

DOI: 10.1017/9781108332699

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First published 2017

Printed in the United Kingdom by Clays, St Ives plc

*A catalogue record for this publication is available from the British Library.*

ISBN 978-1-108-41313-8 Paperback

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## Contents

<i>Preface</i>	<i>page xi</i>
<b>1 Relations among partitions</b> <i>R. A. Bailey</i>	1
<b>2 Large-scale structures in random graphs</b> <i>Julia Böttcher</i>	87
<b>3 The spt-function of Andrews</b> <i>William Y. C. Chen</i>	141
<b>4 Combinatorial structures in finite classical polar spaces</b> <i>Antonio Cossidente</i>	204
<b>5 Switching techniques for edge decompositions of graphs</b> <i>Daniel Horsley</i>	238
<b>6 Ramsey-type and amalgamation-type properties of permutations</b> <i>Vít Jelínek</i>	272
<b>7 Monotone cellular automata</b> <i>Robert Morris</i>	312
<b>8 Robustness of graph properties</b> <i>Benny Sudakov</i>	372
<b>9 Some applications of relative entropy in additive combinatorics</b> <i>Julia Wolf</i>	409

## Preface

The Twenty-Sixth British Combinatorial Conference was held at the University of Strathclyde in Glasgow in July 2017. The British Combinatorial Committee had invited nine distinguished combinatorialists to give survey lectures in their areas of expertise, and this volume contains the survey articles on which these lectures were based.

In compiling this volume, we are very grateful to the authors for preparing their excellent surveys so professionally, and to the anonymous referees for their detailed and timely responses. We would also like to thank the team at Cambridge University Press, in particular Roger Astley, Clare Dennison and Abigail Walkington, for all their assistance and advice. Finally, we could not have completed this task without the experience of the editors of earlier volumes of Surveys and the guidance of the British Combinatorial Committee.