

1 Integers



Exercise 1.1 Using negative numbers

- 1 Hassan is comparing the temperatures in five cities, on the same day. He recorded them in degrees Celsius (°C).
Write the temperatures in order, starting with the highest.

-5 5 -4 3 -1

- 2 Anders recorded the temperature in his greenhouse, in degrees Celsius, at five different times on the same day.

Time	09 00	11 00	13 00	16 00	19 00
Temperature (°C)	-8	-5	2	1	-3

- a What time was the lowest temperature?
b What time was the highest temperature?
c What was the difference in temperature between 11 00 and 16 00?
- 3 What temperature is halfway between each pair?
a 6 °C and -2 °C b -12 °C and -4 °C
- 4 At 08 00, the temperature in Harsha’s garden was -5 °C.
During the day the temperature rose by 8 degrees and then, by 22 00, it fell by 3 degrees.
What was the final temperature?
- 5 Sasha writes the height of a point that is 50 metres below sea level as -50 metres.
a How does she write a height that is 200 metres lower than that?
b How does she write a height that is 200 metres higher than that?
- 6 Albert notices that his freezer is getting colder by 4 degrees every minute.
The temperature now is 6 °C.
What will the temperature be in 5 minutes?
- 7 Work these out.
a -2 + 6 b -10 + 3 c -5 + 5
d -3 + 13 e -6 + 5 + 3
- 8 Find the solutions.
a 2 - 6 b 5 - 12 c -6 - 3
d -9 - 2 e -3 - 6 - 6
- 9 Complete these calculations.
a -3 + 2 - 4 = b 3 - 5 + 6 =
c 8 + 3 - 12 = d -7 + 5 - 3 + 2 =



Exercise 1.2 Adding and subtracting negative numbers

- 1 Work out the following additions.
a $4 + 7$ b $4 + -7$ c $-4 + 7$ d $-4 + -7$
- 2 Work out these subtractions.
a $8 - 12$ b $3 - -4$ c $-5 - -7$ d $-6 - -3$
- 3 Find the solutions.
a $3 - 10$ b $5 + -6$ c $8 + -5$ d $-4 - -5$
- 4 Find the missing numbers.
a $4 - \square = -3$ b $-2 + \square = 5$ c $\square + -5 = 2$ d $\square - 5 = -3$
- 5 The difference between two temperatures is 8 degrees.
One temperature is 3°C .
What is the other temperature?
- 6 Xavier is thinking of two numbers.

The sum of my two numbers is 4.
One of my numbers is -6.



There are two possible answers.
Try to find both of them.

What is Xavier’s other number?

- 7 Copy and complete this addition table.

+	4	1	-2
3			1
-1			
-3		-2	

The two entries show that $3 + -2 = 1$ and $-3 + 1 = -2$. You must fill in the rest.

Exercise 1.3 Multiples

- 1 Write down the first five multiples of each number.
a 9 **b** 12 **c** 20
 - 2 **a** Find the fourth multiple of 6.
b Find the sixth multiple of 4.
 - 3 From the numbers in the box, find a multiple of:
a 8 **b** 10 **c** 11 **d** 13.
- 20 26 32 38 44
- 4 Find a number between 40 and 50 that is:
a a multiple of 7 **b** a multiple of 12 **c** a multiple of 14.
 - 5 The 16th multiple of 7 is 112.
a What is the 17th multiple of 7? **b** What is the 15th multiple of 7?
 - 6 Find the lowest common multiple of the numbers in each pair.
a 3 and 5 **b** 6 and 8 **c** 10 and 15 **d** 4 and 7
 - 7 Maha has a number of apples.

I could share my apples equally
among 3, 4 or 5 people.



What is the smallest number of apples Maha could have?

- 8 **a** What is the third multiple of 167?
b What are the sixth and ninth multiples of 167?

Exercise 1.4 Factors and tests for divisibility




- Two of the factors of 24 are 1 and 24.
Find all the other factors.
- Find all the factors of each of these numbers.
a 8 **b** 12 **c** 21 **d** 17 **e** 40
- 3 6 16 26 36 46

 Which numbers in the box have 3 as a factor?
- There are two numbers between 30 and 40 that have just two factors.
What are they?
- Find the four factors of 91.
- Find the common factors of each pair of numbers.
a 12 and 15 **b** 20 and 30 **c** 8 and 24 **d** 15 and 32
- Find a number that has exactly:
a 3 factors **b** 5 factors.
- 2571 5427 6622 8568

 Which numbers in the box are multiples of:
a 3 **b** 9?
- 2884 2885 2886 2887 2888

 From the list of numbers in the box, find the multiples of:
a 4 **b** 5 **c** 6 **d** 8 **e** 10.
- What is the smallest number that has 2, 3, 4, 5 and 6 as factors?
- Find the number less than 100 that has the largest number of factors.

Exercise 1.5 Prime numbers

- How many prime numbers are less than 20?
- What is the 15th prime number, if they are listed in order?
- List all the prime numbers between 80 and 90.
-  Explain why a prime number cannot be a square number.
-  Are these statements true or false?
a All primes are odd numbers.
b It is impossible to find three consecutive odd numbers that are all primes.
c There is only one prime number between 90 and 100.
-  **a** Write 25 as the sum of three different prime numbers.
b How many ways are there to do this?

- 7 Find the prime factors of each number.
a 12 b 27 c 28 d 30
- 8 Write each of these numbers as a product of primes.
a 21 b 22 c 35 d 51 e 65

Prime factors are factors that are prime numbers.



- 9 Why can two prime numbers only have one common factor?

Exercise 1.6 Squares and square roots

- 1 Find the value of each number.
a 5^2 b 9^2 c 11^2 d 18^2
- 2 There is one square number between 200 and 250.
What is it?
- 3 Find two square numbers that add up to each of these numbers.
a 80 b 90 c 100



- 4 Look at the pattern in the box.
a Check that it is correct.
b Write down the next two lines in the pattern.
c Use the pattern to work out $51^2 - 49^2$.

$$\begin{aligned} 4^2 - 2^2 &= 2 \times 6 \\ 5^2 - 3^2 &= 2 \times 8 \\ 6^2 - 4^2 &= 2 \times 10 \end{aligned}$$



- 5 The difference between two square numbers is 19.
What are the two square numbers?
- 6 The sum of two square numbers is 15^2 .
What are the square numbers?
- 7 There are nine square numbers less than 100.
Which one has the largest number of factors?
- 8 Find the value of each number.
a $\sqrt{9}$ b $\sqrt{36}$ c $\sqrt{169}$ d $\sqrt{400}$ e $\sqrt{256}$
- 9 Is $\sqrt{9+16}$ the same as $\sqrt{9} + \sqrt{16}$?
Give a reason for your answer.
- 10 The square root of Eve's age is two more than the square root of Jamil's age.
If Jamil is 9 years old, how old is Eve?

2 Sequences, expressions and formulae

Exercise 2.1 Generating sequences (1)

- 1 For each of these infinite sequences, write down:
- i the term-to-term rule
 - ii the next two terms
 - iii the tenth term.
- a 12, 14, 16, 18, ... b 5, 8, 11, 14, ... c 46, 42, 38, 34, ...
- 2 Write down the first three terms of each of these sequences.

	First term	Term-to-term rule
a	4	Add 3.
b	30	Subtract 5.
c	15	Add 3 and then subtract 4.
d	10	Multiply by 2 and then add 1.
e	2	Divide by 2 and then add 10.
f	12	Multiply by 2, then divide by 4 and then multiply by 2.

- 3 Copy these finite sequences.
Fill in the missing terms that go in the boxes.
- a 6, 9, , 15, , 21, 24 b 3, 10, 17, , , 38,
- c 45, , , 27, 21, , 9 d , , 17, 14, , ,
- 4 Write down whether each of these sequences is finite or infinite.
- a 5, 10, 15, 20 b 3, 5, 7, 9, ... c 585, 575, 565, 555



- 5 Anders and Tanesha are looking at this number sequence.
3, 6, 17, 42, 87, 158, ..., ...
Is either of them correct?
Explain your answer.



I think the term-to-term rule is: 'Add 3.'



I think the term-to-term rule is: 'Multiply by 2.'



- 6 The second term of a sequence is 10.
The term-to-term rule is: 'Multiply by 4 then subtract 2.'
What is the first term of the sequence?

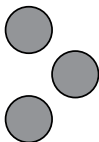


- 7 The fourth term of a sequence is 18.
The term-to-term rule is: 'Subtract 3 then multiply by 3.'
What is the first term of the sequence?

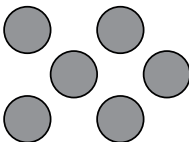
Exercise 2.2 Generating sequences (2)

1 This pattern is made from dots.

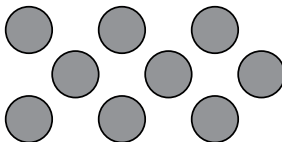
Pattern 1



Pattern 2



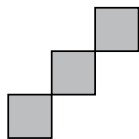
Pattern 3



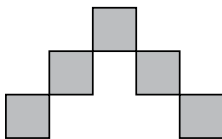
- a Draw the next two patterns in the sequence.
- b Write down the number sequence of the dots.
- c Write down the term-to-term rule.
- d Explain how the sequence is formed.

2 This pattern is made from squares.

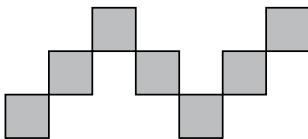
Pattern 1



Pattern 2



Pattern 3



- a Draw the next two patterns in the sequence.
- b Copy and complete the table to show the number of squares in each pattern.

Pattern number	1	2	3	4	5
Number of squares	3	5			

- c Write down the term-to-term rule.
- d How many squares will there be in:
 - i Pattern 8
 - ii Pattern 15?

3 This pattern is made from blocks.

Pattern 1



Pattern 2




Pattern 3

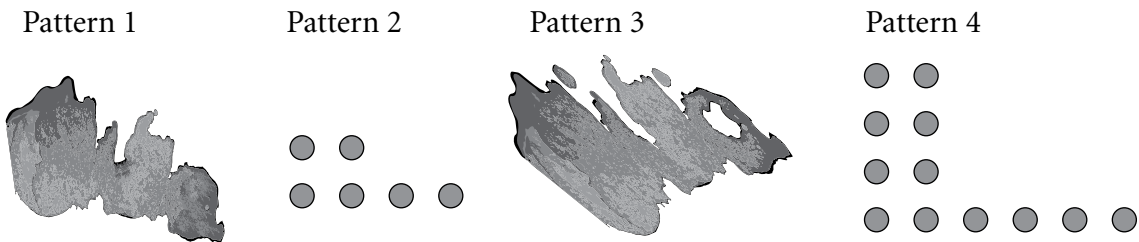


- a Draw the next two patterns in the sequence.
- b Copy and complete the table to show the number of blocks in each pattern.


Pattern number	1	2	3	4	5
Number of blocks					

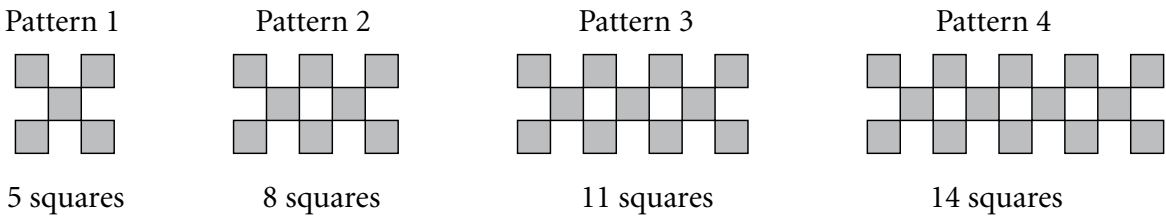
- c Write down the term-to-term rule.
- d How many blocks will there be in:
 - i Pattern 10
 - ii Pattern 20?

-  **4** Sesane is using dots to draw a sequence of patterns. She has spilt coffee over the first and third patterns in her sequence!



- a** Draw the first and the third patterns of Sesane’s sequence.
b How many dots will there be in Pattern 6?

-  **5** Alicia and Oditi are looking at this sequence of patterns made from squares.



I think there are 23 squares in Pattern 20 because the pattern is going up in threes, and $20 + 3 = 23$.

I think there are 62 squares in Pattern 20 because if I multiply the pattern number by 3 and add 2 I always get the number of squares. $20 \times 3 + 2 = 62$.



Who is correct? Explain your answer.

Exercise 2.3 Representing simple functions

1 Copy these function machines and find the missing inputs and outputs.

a

Input		Output
3	$+ 5$...
7		...
...		14

b

Input		Output
10	$- 7$...
...		7
20		...

c

Input		Output
10	$\times 5$...
...		35
...		100

2 Copy these function machines and find the missing inputs and outputs.

a

Input			Output
3	$+ 3$	$\times 3$...
...			30
...			27

b

Input			Output
3	$\times 3$	$+ 3$...
...			30
...			27

c

Input			Output
3	$- 2$	$\div 2$...
...			6
...			12

3 Work out the rule to complete these function machines.

a

Input		Output
3	...	6
7		10
11		14

b

Input		Output
15	...	5
21		7
30		10

c

Input		Output
3	...	21
5		35
7		49

4 Copy and complete the mapping diagram below for this function machine.

Input		Output
3	$+ 4$	7
5		9
6		10

Input	0	1	2	3	4	5	6	7	8	9	10
Output											

5 Jake and Hassan look at this function machine.

Input			Output
3	3
5			7
9			15

Test the input numbers in each of their functions to see if either of them is correct.

Jake says: 'I think the function is multiply by 2 then take away 3.'
Hassan says: 'I think the function is multiply by 3 then take away 3.'
Who is correct? Explain your answer.

6 Razi draws this mapping diagram and function machine of the same function.

Input	0	1	2	3	4	5	6	7	8	9	10
Output	0	1	2	3	4	5	6	7	8	9	10

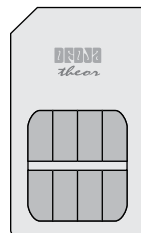
Input			Output
...
...			...
...			...

Fill in the missing numbers and write the rule in the function machine.

Exercise 2.4 Constructing expressions

- 1** Shen has a box that contains t toys.
 Write an expression for the total number of toys he has in the box when:
- a** he puts in 4 more **b** he takes 2 out
c he adds 5 **d** he takes out half of them.
- 2** Dafydd has a bag with s sweets in it.
 Write an expression for someone who has a bag with:
- a** 2 more sweets than Dafydd **b** 3 times as many sweets as Dafydd
c 6 fewer sweets than Dafydd **d** half as many sweets as Dafydd.
- 3** Write down an expression for the answer to each of these.
- a** Ali has x paintings. He buys 2 more.
 How many paintings does he now have?
- b** Hamza has t free SMS's on his mobile phone each month.
 So far this month he has used 15 SMS's.
 How many free SMS's does he have left?
- c** Ibrahim is i years old and Tareq is t years old.
 What is the total of their ages?
- d** Aya can store v video clips on one memory card.
 How many video clips can he store on 2 memory cards?
- e** Rania is given \$ d for her birthday.
 She spends a quarter of the money on make-up.
 How much does she spend on make-up?
- 4** Nesreen thinks of a number, n .
 Write an expression for the number Nesreen gets each time.
- a** She multiplies the number by 6. **b** She multiplies the number by 5 then adds 1.
c She multiplies the number by 7 **d** She divides the number by 4.
 then subtracts 2.
- e** She divides the number by 2 **f** She divides the number by 5 then subtracts 3.
 then adds 10.
- 5** The cost of an adult meal in a fast food restaurant is \$ a .
 The cost of a child's meal in the same restaurant is \$ c .
 Write an expression for the total cost of meals for each group.
- a** 1 adult and 1 child **b** 1 adult and 3 children
c 4 adults and 1 child **d** 4 adults and 5 children
- 6** Fatima thinks of a number, n .
 Write an expression for the number Fatima gets each time.
- a** She adds 2 to the number and then multiplies by 3.
b She adds 2 to the number and then divides by 3.
c She subtracts 5 from the number and then multiplies by 4.
d She subtracts 5 from the number and then divides by 4.

In each part of the question Shen starts with t toys.



Remember to use brackets if an addition or a subtraction must be done before a multiplication or a division.