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978-1-107-62154-1 - Localization in Periodic Potentials: From Schrödinger Operators to the Gross–Pitaevskii Equation

Dmitry E. Pelinovsky

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