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978-1-107-62154-1 - Localization in Periodic Potentials: From Schrödinger Operators to the Gross–Pitaevskii Equation

Dmitry E. Pelinovsky

Index

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Index

- Ablowitz–Ladik lattice, 23, 39, 293, 307, 311, 322, 342
- algebraic multiplicity, 43, 199, 231
- anticontinuum limit, 151
- asymmetric vortex configurations, 156–158
- asymptotic multi-scale expansion, 3, 77, 91, 108, 113, 137, 328
- asymptotic stability, 196, 267, 281
- asymptotically hyperbolic operator, 296
- Banach algebra, 34, 79, 102, 316, 351, 365, 376, 384
- Banach Fixed-Point Theorem, 34, 80, 86, 97, 176, 366, 372
- band edge, 63, 129
- beyond-all-orders perturbation theory, 335
- Bloch decomposition, 65, 67, 74, 92, 99
- Bloch waves, 8, 63, 88
- bond-symmetric soliton, 166, 252, 301
- bound states, 118
- Brillouin zone, 64, 94
- Brouwer Fixed-Point Theorem, 367
- Cauchy Integral Theorem, 45
- Cauchy sequence, 366
- Cayley transform, 212
- center manifold, 349, 356
- center manifold reduction, 329
- characteristic exponents, 55
- characteristic function, 100
- codimension-infinity bifurcation, 346
- codimension-one bifurcation, 312
- coercivity condition, 123
- comparison principle, 371
- complex eigenvalues, 210, 227, 228
- concentration compactness principle, 121, 128, 189
- congruent operator, 208
- constrained space, 177, 188, 203, 216, 218, 231, 234, 244, 249, 264, 278
- constrained spaces, 177, 188
- continuous spectrum, 40, 199, 223, 238, 247, 269, 296, 297, 315
- contraction mapping principle, 366
- coupled nonlinear Schrödinger equation, 2, 19, 30, 105, 232, 241, 245
- Cramer’s rule, 248
- cubic discrete nonlinear Schrödinger equation, 293, 328, 342
- cubic nonlinear Schrödinger equation, 38, 39, 48, 275, 291, 347
- differential advance–delay equation, 311, 326
- differential advance–delay operators, 294, 315
- Dirac operator, 85
- Dirac delta function, 58, 102, 274, 299
- discrete breathers, 118
- discrete Gross–Pitaevskii equation, 359
- discrete Klein–Gordon equation, 35, 313, 334
- discrete nonlinear Schrödinger equation, 3, 14, 22, 33, 105, 113, 245, 253, 280
- discrete spectrum, 40, 199, 378
- discrete translational transformation, 23
- disjoint spectral bands, 64
- Duhamel’s principle, 28, 80, 97
- effective potential, 144
- eigenvalues, 199
- embedded eigenvalues, 199, 201, 227, 238, 273, 297
- energy, 17, 25, 31, 119, 153, 168, 189, 193, 232, 277, 301, 376
- essential spectrum, 199, 378, 381
- Euler–Lagrange equation, 375
- excitation threshold, 129
- explicit Euler method, 186
- exponential weighted spaces, 297
- finite-time blow-up, 27
- fixed-point iterations, 29, 92, 110
- Floquet multipliers, 54, 163
- Floquet Theorem, 54, 368
- fold bifurcation, 133
- Fourier transform, 76
- Fréchet derivative, 135
- Fredholm operator, 135, 296, 369
- Fredholm theory, 225

Cambridge University Press

978-1-107-62154-1 - Localization in Periodic Potentials: From Schrödinger Operators to the Gross–Pitaevskii Equation

Dmitry E. Pelinovsky

Index

[More information](#)

396

Index

- Fredholm Alternative Theorem, 41, 86, 89, 92, 300, 332, 355, 370
 fundamental localized modes, 144, 247
 fundamental vortex, 242
- Gagliardo–Nirenberg inequality, 32, 120, 124, 371
- Galileo transformation, 22
 gap solitons, 118, 172, 261
 gauge transformation, 19, 23, 116, 119, 151
- Gateaux derivative, 16
 generalized discrete nonlinear Schrödinger equation, 292, 301, 308, 311, 312, 322
 generalized eigenvalue problem, 197, 207, 214, 218, 234, 244, 250, 264
 generalized Gross–Pitaevskii equation, 267
 generalized nonlinear Schrödinger equation, 215, 242
 geometric multiplicity, 43, 199, 231
 global well-posedness, 26, 31, 34, 36
 Gram–Schmidt orthogonalization, 378
 Green’s function, 200, 202
 Gronwall inequality, 34, 81, 97, 358, 371
 Gross–Pitaevskii equation, 1, 4, 73, 88, 105, 118, 137, 185, 195, 229, 241, 291, 346, 376
 Gross–Pitaevskii equation with periodic coefficients, 7, 11, 15, 24
 Gross–Pitaevskii equation with power nonlinearity, 281
 Gross–Pitaevskii equation with quadratic nonlinearity, 81
 Gross–Pitaevskii equation with separable potential, 105, 117
- Hölder inequality, 104
 Hamiltonian system, 15, 16, 193, 309, 350
 Heaviside step function, 206
 Hermite functions, 11
 Hessian matrix, 233
 Hessian operator, 195
 heteroclinic orbit, 168
 homoclinic orbit, 167, 352
 hyperbolic operator, 296
 hypergeometric equation, 235
- ill-posedness, 26
 imaginary-time integration method, 185
 implicit Crank–Nicholson method, 190
 implicit Euler method, 189
 Implicit Function Theorem, 84, 100, 104, 115, 132, 315, 357, 372
 infinitesimal symmetry generator, 18
 inhomogeneous systems, 48
 initial-value problem, 26
 integrable equations, 37
 inter-site soliton, 166, 301
 inverse scattering transform method, 37
 involution, 166
 isolated eigenvalues, 42, 201, 225, 296
- Jacobian operator, 131, 255
 Jordan block decomposition, 220, 225
 kinks, 167, 310
 Kronecker symbol, 58, 100
- Lagrange multipliers, 125, 189, 193, 203
 Laplace transform, 330, 338
 Lax equation, 39
 linear Gross–Pitaevskii equation, 268
 linear Schrödinger equation, 5, 8, 235, 238
 linear wave–Maxwell equation, 50
 linearized stability, 195, 266
 local well-posedness, 26, 27, 33, 35, 78, 97, 111
 Lyapunov stability, 267, 278, 280
 Lyapunov–Schmidt reduction method, 131, 236, 254
- Manakov system, 20, 38, 240
 massive Thirring model, 39
 maximal non-positive subspace, 211, 226
 Melnikov integral, 322
 momentum, 21, 25, 233, 309, 376
 monodromy matrix, 54
 Mountain Pass Theorem, 128, 374
 multi-component nonlinear Dirac equations, 25, 37
 multi-pulse localized modes, 145, 180
 multiple eigenvalues, 199, 211, 224, 226, 228, 230
- near-identity transformations, 17
 Neumann series, 42
 neutral subspace, 226
 Noether Theorem, 21, 375
 non-autonomous systems, 48
 non-positive subspace, 211
 non-resonance conditions, 92
 nonlinear Dirac equations, 2, 6, 23, 35, 73, 168, 261
 nonlinear Dirac equations with quintic nonlinearity, 173
 nonlinear Klein–Gordon equation, 7, 10, 14, 359
 nonlinear oscillator equation, 57
 nonlinear Schrödinger equation, 1, 10, 88, 137
 nonlinear Schrödinger equation with power nonlinearity, 32
 nonlinear Schrödinger equation with variable coefficients, 48
 nonlinear wave–Maxwell equation, 7
 normal coordinates, 351
 normal form, 328, 352
 normal form transformation, 91, 108
 norming constant, 42
- on-site soliton, 166, 301
 orbital stability, 196, 266, 277
 overlapping spectral bands, 64

Cambridge University Press

978-1-107-62154-1 - Localization in Periodic Potentials: From Schrödinger Operators to the Gross–Pitaevskii Equation

Dmitry E. Pelinovsky

Index

[More information](#)*Index*

397

- Palais–Smale compactness condition, 127, 374
- Parseval's equality, 28, 59, 65, 67, 70
- Peierls–Nabarro barrier, 301
- perturbation theory, 220, 247
- Petviashvili's method, 173
- Picard–Kato method, 26
- planar Hamiltonian system, 16, 170, 352
- Plancherel Theorem, 365
- Plemelej's projection operators, 45
- point transformation, 48, 160
- Pontryagin space, 211, 222
- Pontryagin Invariant Subspace Theorem, 198, 211
- power, 18, 19, 25, 31, 119, 139, 153, 217, 233, 277, 376
- power map, 174, 178
- quadratic eigenvalue problem, 257
- quadratic form, 207
- quasi-momentum, 63
- Rayleigh quotient, 121, 187, 192, 251
- remainder term, 91
- residual term, 91
- resonance, 273, 346
- resonant Fourier modes, 5, 88
- reversibility, 351, 358
- Riemann surface, 270
- Riemann–Hilbert problem, 45
- Riemann–Lebesgue Lemma, 66, 78, 376
- Riesz Representation Theorem, 381
- rotational symmetry, 20, 241
- saddle-node bifurcation, 133
- Salerno model, 293, 323, 335
- scaling transformation, 101, 140, 150
- scattering coefficients, 41
- scattering data, 201, 272, 298, 315
- Schauder Fixed-Point Theorem, 214, 367
- Schrödinger operator, 53, 88, 103, 198, 215, 229, 233, 268
- semi-simple eigenvalues, 199, 224
- separable Hilbert space, 381
- sesquilinear form, 223
- shooting method, 163
- site-symmetric soliton, 166, 301
- Sobolev Embedding Theorem, 31, 59, 72, 76, 119, 371, 376
- solitary waves, 118
- soliton configuration, 151, 156, 157, 245, 259
- solitons, 38, 47, 98, 215, 232, 240, 291, 347
- spectral band, 63, 346
- spectral gap, 63, 129
- Spectral Mapping Theorem, 55, 367
- spectral renormalization method, 174
- spectral stability, 195, 215, 230
- Spectral Theorem, 53, 58, 198, 378
- stable manifold, 167, 338, 349, 356, 379
- Stable Manifold Theorem, 379
- staggering transformation, 150, 165
- stationary cubic nonlinear Schrödinger equation, 232, 235
- stationary discrete nonlinear Schrödinger equation, 114, 117, 122, 150, 301
- stationary discrete nonlinear Schrödinger equation with power nonlinearity, 164
- stationary discrete nonlinear Schrödinger equation with saturable nonlinearity, 168
- stationary generalized Gross–Pitaevskii equation, 268
- stationary generalized nonlinear Schrödinger equation, 164, 215, 242
- stationary Gross–Pitaevskii equation, 81, 87, 98, 114, 119, 133, 137, 174, 229
- stationary Gross–Pitaevskii equation with a fourth-order dispersion, 147
- stationary Gross–Pitaevskii equation with periodic coefficients, 160
- stationary Gross–Pitaevskii equation with power nonlinearity, 162
- stationary nonlinear Dirac equations, 81
- stationary nonlinear Schrödinger equation, 98, 166, 352
- stationary nonlinear Schrödinger equation with power nonlinearity, 170, 206, 208
- Stokes constant, 336, 341
- Strichartz's estimates, 285
- Strichartz's pair, 284
- strong convergence, 123, 380
- strong stationary solution, 119, 133, 135, 163
- Sturm Comparison Theorem, 203, 378
- Sturm–Liouville problem, 57
- Sylvester Law of Inertia, 198, 207, 250
- symmetric vortex configurations, 156–158
- symmetry reductions, 160
- symplectic form, 16
- symplectic inner product, 273
- symplectic linear transformations, 17, 20
- symplectic orthogonality, 282
- tangent bifurcation, 133
- tight-binding approximation, 106
- translational transformation, 22, 137
- translationally invariant localized modes, 301
- twisted soliton, 252
- unstable manifold, 167, 338, 349, 379
- Unstable Manifold Theorem, 163, 167, 379
- Vakhitov–Kolokolov criterion, 217
- vortex cell, 155, 258
- vortex charge, 155
- vortex configurations, 254, 259
- vortex cross, 159, 261
- vortices, 134

Cambridge University Press

978-1-107-62154-1 - Localization in Periodic Potentials: From Schrödinger Operators to the Gross–Pitaevskii Equation

Dmitry E. Pelinovsky

Index

[More information](#)

398

Index

Wannier decomposition, 70, 114

Wannier functions, 12, 69

weak convergence, 123, 380

Weak Convergence Theorem, 123, 128, 381

weak stationary solution, 119, 120

weakly lower semi-continuity, 124

Weierstrass Theorem, 305

weighted inner product, 243

Weyl Theorem, 40, 201, 247, 269, 297, 381

Wiener algebra, 376, 384

Wiener space, 76

WKB solution, 12

Wronskian, 41, 54, 272

Young's inequality, 365