

*Astrophysical Masers:
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Malcolm Walmsley's Maser Science

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Charles Malcolm Walmsley passed away on 1 May 2017. Over a long and highly productive career, Malcolm made numerous and fundamental contributions to the science of the interstellar medium and star formation. These have recently been summarized elsewhere (Menten & Cesaroni 2017). Here I would like to describe some of his work related to masers.

Malcolm became strongly engaged in astronomical maser research in the mid-1980s, when a relatively strong and narrow spectral line from the methanol molecule (CH_3OH) at 23.1 GHz was serendipitously discovered with the Effelsberg 100 meter radio telescope of the Max-Planck-Institut für Radioastronomie (MPIFR). At that time, the only known methanol maser lines were the series of $J_{k=2} - J_{k=1}$ transitions of *E*-type CH_3OH ($J = 2, 3, 4, \dots$) near 25 GHz that had *only* been found in the Orion Kleinmann-Low nebula in 1971 by Barrett *et al.* (1971) and nowhere else, despite extensive searches. It became clear that toward Orion-KL, the newly detected 23.1 GHz line was *not* masing, although it was detected there. The title of the article, by Wilson *et al.* (1984), reporting this line, *Detection of a new type of methanol maser*, gave the first hint at the class I/class II methanol maser dichotomy – the 23.1 GHz $9_2 - 10_1 A^+$ being the first class II line, to which soon the even stronger 19.9 GHz $2_1 - 3_0 E$ line was added (Wilson *et al.* 1985). In contrast, the 25 GHz lines belong to class I.

These discoveries triggered Malcolm's interest in methanol masers, which became a major portion of my dissertation that he had started supervising. With the great sensitivity of Effelsberg, more 25 GHz maser sources were detected in regions much farther away than Orion (Menten *et al.* 1986). Malcolm also became curious about the excitation of methanol masers. At that time, collisional rate coefficients didn't exist for CH_3OH , so he used what published (experimental) information he could find in the literature and conducted statistical equilibrium calculations that indeed predicted maser action in the class I maser lines newly discovered by Morimoto *et al.* (1985) with the Nobeyama 45 meter telescope. Most interestingly, these calculations also predicted enhanced absorption against the cosmic microwave background (“over-cooling”) in the 12.1 GHz $2_0 - 3_{-1} E$ transition toward cold dark clouds. This he indeed discovered toward two objects, a result he particularly cherished (Walmsley *et al.* 1988). Toward high-mass star forming regions with strong far infrared (FIR) radiation he and his collaborators had found this line to be the (then) strongest class II methanol maser line (Batra *et al.* 1987).

At that time, Malcolm also was studying hyperfine structure (hfs) lines from rotationally excited levels of the hydroxyl radical (OH) at multiple radio frequencies, also with the Effelsberg telescope and with the VLA and VLBI (e.g., Walmsley *et al.* 1986). A conclusion of this work is a comprehensive study of OH excitation (with R. Cesaroni) that consisted of innovative statistical equilibrium calculations (considering FIR line overlaps; Cesaroni & Walmsley 1991). It was aimed at reproducing the observed pattern of maser emission in some hfs lines and absorption in others and constrained the physical conditions in the OH-bearing regions, i.e. the warm, dense molecular envelopes of ultracompact HII regions, which also harbor class II CH_3OH masers.

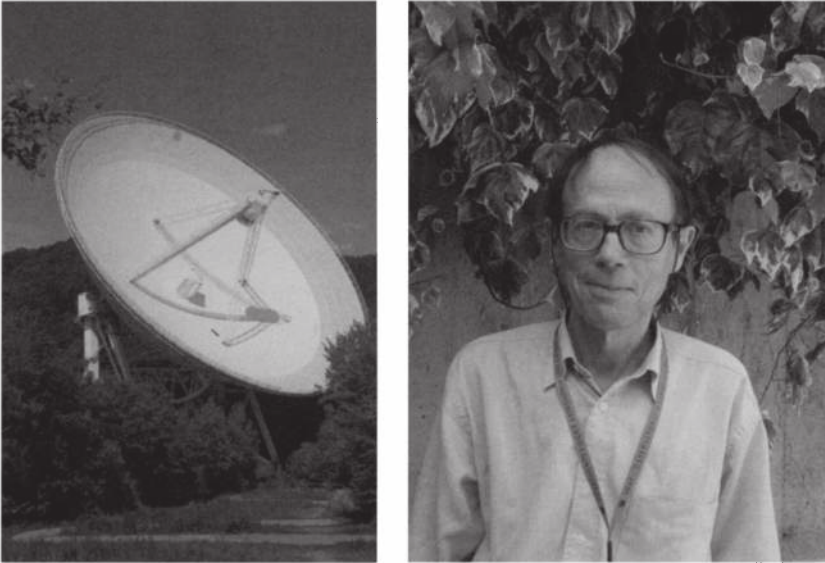


Figure 1. The MPIfR 100 meter radio telescope at Effelsberg, Germany. It started operations in 1972 and was extensively used by Malcolm Walmsley, his collaborators and students for a wide range of studies on interstellar radio recombinations lines and molecules. The picture of Malcolm was taken in 2005 in Acireale on Sicily at the IAU Symposium 227 *Massive star birth: A Crossroads of Astrophysics*, a conference he co-organized. Credits: MPIfR/N. Junkes and Cambridge University Press

The above work was done while Malcolm was a staff member of the MPIfR in Bonn, where he worked from 1969–1994. During the second part of his career, at Arcetri Observatory, he collaborated in numerous projects on high mass star forming regions, many of which involved masers. Finally, in one of his last papers, he returned to the topic of class I methanol masers and made major contributions to a comprehensive study of their excitation. It was published 30 years after his first paper on the subject (Leurini *et al.* 2016, see also the contribution by Leurini & Menten to these proceedings).

Malcolm Walmsley was invited to give the summary talk at this conference, a task he sadly could not perform. This meeting has been dedicated to his memory.

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Maser Theory: Old Problems and New Insights

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Abstract. Maser theory continues to be driven by advances in observational techniques. Here, I consider the responses to VLBI with space-Earth baselines and cross-correlation spectroscopy (a re-consideration of coherence properties), routine observation in full-Stokes polarization (a re-casting of the polarization transfer equations), and long-term variability monitoring (3-D modelling of irregular domains).

Keywords. masers, molecular processes, radiative transfer, ISM: molecules, radio lines: general

1. Introduction

I consider in detail three areas of active maser research that may benefit from some new, or re-discovered, theoretical insight in addition to the available observational data. These areas are the coherence properties of astrophysical masers, the modelling of maser polarization, and the analysis of maser variability with 3-D radiative transfer and saturation models.

2. Coherence Properties

Two types of coherence are discussed in Elitzur (1992): phase coherence and bandwidth coherence. Phase coherence is maintained between two rays from some point on a source, diverging through some beam angle θ , and propagated over a distance L , provided that the phase difference $\Delta\phi = L\pi\theta^2/\lambda$ is much smaller than 1 radian. Large values of L , of order 10^{12} m in astrophysical masers, drove the conclusion that astrophysical masers are not phase coherent. This probably remains a valid conclusion, but the recent detection, with an interferometer including the RadioAstron instrument, of a 22-GHz ($\lambda = 0.0136$ m) H_2O maser in Cep A that is unresolved at an angular scale of $10 \mu\text{as}$, improves the condition by several orders of magnitude. At the distance of Cep A, this angular scale corresponds to a linear distance of $\sim 10^9$ m. Using this distance as L , but keeping the original estimate of $\pi\theta^2 = 3.14 \times 10^{-4}$, we obtain $\Delta\phi = 2.42 \times 10^6$, so the conclusion of no phase coherence still appears safe, even with the smallest maser features so far discovered.

The second type of coherence discussed in Elitzur (1992) is bandwidth coherence. For a source to be bandwidth coherent, the essential requirement is that the homogeneous response profile of the transition is broader than the inhomogeneous profile. The homogeneous profile broadens as a maser saturates due to power, or saturation, broadening. This arises from Stark effect distortion of the molecule by the electric field of the maser radiation. According to Elitzur (1992), power broadening becomes sufficient to enforce bandwidth coherence for a brightness temperature of $T_b > 3 \times 10^{14} (4\pi/\Omega)$ K for the

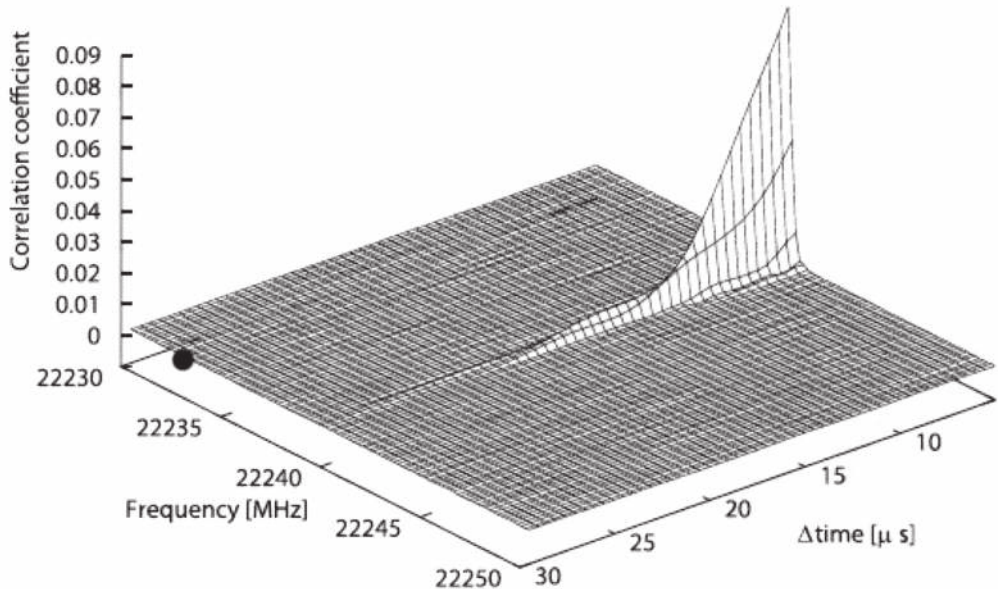


Figure 1. The coherence function as a function of time delay and of frequency across the line in an observation of the star-forming region W3(H₂O) by Takefugi *et al.* (2016)

22-GHz transition of H₂O. For reasonable maser beam angles, see above, the brightest maser sources, particularly flares, could be marginally bandwidth coherent. For example water-maser flares have been observed in Orion with $T_b > 10^{16}$ K (Kobayashi *et al.* 2000), and with $T_b \simeq 8 \times 10^{17}$ K (Strel'nitskii 1982).

Recent evidence from observationally measured coherence functions (Takefugi *et al.* 2016) strongly suggests that very bright astrophysical masers are indeed bandwidth coherent. The key point is the shape of the decay of the coherence function (Fig. 1), which has a long tail towards longer time delays that is inconsistent with the Gaussian behaviour expected if the function were controlled by the inhomogeneous profile. Note that the relation between the coherence function and the line shape is a Fourier transform: a Gaussian inhomogeneous profile transforms to a Gaussian decay in the coherence function; a Lorentzian homogeneous profile transforms to an exponential, with a much slower decay. The observed coherence time in this example is 18 μ s, suggesting a homogeneous width of 56 kHz. This compares to an observed inhomogeneous line profile width (full width at half power) of 96 kHz.

The Stark broadening effect by the electric field of the maser radiation imposes an ultimate limit on the brightness temperature, above which the line will be split into a distinctive pattern (Slysh 2003). The fact that a pattern of this type has not been observed suggests that maser beam angles for the brightest sources are of order 10^{-3} , somewhat smaller than the estimates in Elitzur (1992). The measured coherence times in Takefugi *et al.* (2016) indicate that the brightness temperatures of some H₂O maser features in W3(H₂O) and W49 reach 8.5×10^{18} and 6.2×10^{22} K respectively.

Another old, but excellent, reference that covers many aspects of Doppler-broadened maser propagation, including the statistics of the observed radiation, which is related to the work described above, is Menegozzi & Lamb (1978).

3. Polarization

Perhaps no aspect of theoretical maser research has been more controversial. In particular, the case of Zeeman splittings small compared to the inhomogeneous line width has historically been very problematic. Another major source of difficulty is the use of different conventions to describe left- and right-handed polarization, and in the definitions of the Stokes parameters, particularly Stokes- V . Definitions conforming to the IEEE definition of right- and left-handed polarization and the IAU convention for Stokes V are set out in Green *et al.* (2014).

One of the reasons that the polarization problem is so difficult is that four, coupled, simultaneous radiative transfer equations must be solved to recover the Stokes parameters. A piece of old insight into this problem was provided by Landi Degl’Innocenti (1987), who developed a method of writing the Stokes problem in the style of the integrating factor method that is used to write a formal solution of the scalar radiative transfer equation. The result is a Stokes vector solution that may be frequency and/or angle averaged as necessary, allowing the polarization problem to be cast into a Milne-Schwarzschild integral equation form, see, for example, King & Florance (1964), by eliminating the radiation averages from the density matrix (DM) equations.

In detail, Landi Degl’Innocenti solves the full polarization radiative transfer equation, $d\mathbf{i}/d\tau = \boldsymbol{\eta}\mathbf{i}$, in this case assuming negligible spontaneous emission, as $\mathbf{i}(\tau) = \mathbf{O}(\tau, \tau')\mathbf{i}(\tau')$, where τ is the optical depth and $\mathbf{O}(\tau, \tau')$ is a 4×4 matrix operator, the propagation operator that relates the dimensionless Stokes vector, $\mathbf{i}(\tau)$, at two different depths. In the limit where $\tau' \rightarrow 0$, this operator multiplies the Stokes vector for a ray just entering the maser medium, and can be shown to be equal to (Landi Degl’Innocenti 1987),

$$\mathbf{O}(\tau, \tau') = \mathbf{I} + \sum_{n=1}^{\infty} \frac{1}{n!} \int_{\tau'}^{\tau} d\tau_1 \int_{\tau'}^{\tau_1} d\tau_2 \dots \int_{\tau'}^{\tau_{n-1}} d\tau_n P \{ \boldsymbol{\eta}(\tau_1)\boldsymbol{\eta}(\tau_2)\dots\boldsymbol{\eta}(\tau_n) \} \quad (3.1)$$

In eq. 3.1, \mathbf{I} is the identity matrix, and P is an operator that orders the Stokes matrices, $\boldsymbol{\eta}$ by depth, with the greatest depth on the left. A general Stokes matrix has seven unique elements, and may be written,

$$\boldsymbol{\eta} = \begin{bmatrix} \eta_i & \eta_q & \eta_u & \eta_v \\ \eta_q & \eta_i & \rho_v & -\rho_u \\ \eta_u & -\rho_v & \eta_i & \rho_q \\ \eta_v & \rho_u & \rho_q & \eta_i \end{bmatrix} \quad (3.2)$$

where many models assume $\eta_u = \rho_v = \rho_q = \rho_u = 0$. The remaining terms, η_i, η_q and η_v are functions of the molecular populations or inversions and trigonometrical functions of the angle between the magnetic field, at a certain depth, and the ray direction, possibly with an additional continuum component.

Radiation averages derived from eq. 3.1 can now be used to eliminate these quantities from the DM equations. Such averages, denoted by an over-bar may be grouped into the convenient functions,

$$\begin{aligned} f^{0,\pm} &= \frac{1}{4\pi} \oint 2(\bar{i}^{0,\pm} - \bar{q}^{0,\pm}) \sin^2 \theta d\Omega \\ h^{0,\pm} &= \frac{1}{4\pi} \oint 2\bar{v}^{0,\pm} \cos \theta d\Omega \\ g^{0,\pm} &= \frac{1}{4\pi} \oint [(1 + \cos^2 \theta)\bar{i}^{0,\pm} + \bar{q}^{0,\pm} \sin^2 \theta] d\Omega, \end{aligned} \quad (3.3)$$

where the superscripts denote the transition type of the line shape function that has been used for the frequency integration. The DM equations that the results from eq. 3.3 need to be inserted into are somewhat complicated, but for a 3D model under the complete redistribution approximation, they are

$$\begin{aligned} \Delta^+ &= \frac{\alpha^+}{D} \left\{ (1 + 2f^0) \left[1 - \frac{\alpha^-}{\alpha^+} (g^+ + h^+) + 2(g^- + h^-) \right] + \left(\frac{\alpha^-}{\alpha^+} f^+ - f^- \right) (g^0 + h^0) \right. \\ &\quad \left. + \frac{\alpha^0}{\alpha^+} [f^-(g^+ + h^+) - f^+(1 + 2g^- + 2h^-)] \right\}, \end{aligned} \quad (3.4)$$

where Δ^+ is the inversion in the σ^+ transition of a $J = 1 - 0$ Zeeman group at a specific node or depth of the model. The $\alpha^{\pm,0}$ constants are the ratio of the pump and loss rates for the transition denoted by the superscript. The expression for Δ^- has a similar structure to eq. 3.4, whilst the π -inversion is given by

$$\begin{aligned} \Delta^0 &= \frac{\alpha^0}{D} \left\{ 1 + 2(g^- + h^-) + 2(g^+ - h^+) + 3(g^+g^- - h^+h^-) + 5(g^+h^- - g^-h^+) \right. \\ &\quad - \frac{\alpha^+}{\alpha^0} [g^0(1 + g^- + 3h^-) - h^0(1 + 3g^- + h^-)] \\ &\quad \left. - \frac{\alpha^-}{\alpha^0} [g^0(1 + g^+ - 3h^+) - h^0(1 + 3g^+ + h^+)] \right\}. \end{aligned} \quad (3.5)$$

The denominator, D , common to eq. 3.4 and eq. 3.5 is

$$\begin{aligned} D &= (1 + 2f^0)[1 + 2(g^- + h^-) + 2(g^+ - h^+) + 3(g^+g^- - h^+h^-) + 5(g^+h^- - g^-h^+)] \\ &\quad + f^+[h^0(1 + h^- + 3g^-) - g^0(1 + g^- + 3h^-)] \\ &\quad - f^-[h^0(1 - h^+ + 3g^+) + g^0(1 + g^+ - 3h^+)]. \end{aligned} \quad (3.6)$$

These equations now form a set of non-linear algebraic equations in the $\Delta^{\pm,0}$ at all positions or depths of the model.

4. Nature of Masing Objects

When the physical objects that support astrophysical masers are discussed, we often talk of them as ‘clouds’, but our knowledge of what they actually are is rather limited. An exception is a group of masers found in our own Solar System, known to originate from the comae of comets. The fact that we can reliably use masers for trigonometric parallax distance measurement strongly suggests that at least the masing objects are more like ‘bullet’ clouds than a transient wave-like phenomenon. Clues to the nature of maser objects include the geometry and frequency dependence of their emission, and likely also their variability, since the brightness of maser rays is strongly dependent on the available gain length in the line-of-sight. The considerations above call for a fully 3-D maser model with irregular geometry.

A good way to construct a general 3-D maser model is to use the finite-element method of discretization. Elements can in turn be generated from the Delaunay triangulation of an irregular distribution of points (nodes), see for example Zienkiewicz & Taylor (2000). A triangulated domain of this type is shown in Fig. 2. The radiation solution for all nodes of the domain is carried out via a finite-element implementation of the CEP method (Elitzur & Asensio Ramos 2006, Gray 2012) under a quasi-two-level CVR approximation at present. The solution for a certain optical thickness is straightforwardly used as a starting guess for the next, thicker, model, allowing highly saturated solutions to be

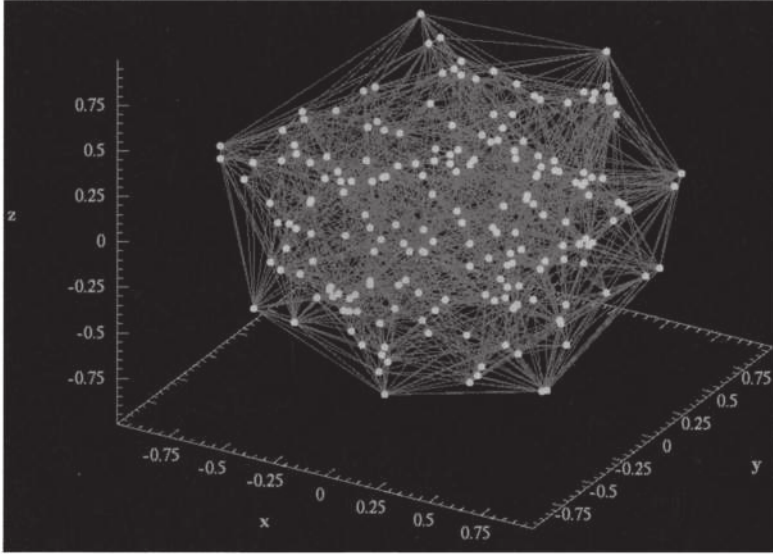


Figure 2. A triangulated domain of 1177 tetrahedral (simplex) elements with 202 nodes

obtained. If the model has J nodes and Q ray paths, then the inversion Δ_i , at the i th node, is given by

$$\Delta_i - \left[1 + \frac{i_{BG}}{4\pi} \sum_{q=1}^Q \frac{a_q}{s_q^2} \sum_{n=0}^{\infty} \frac{1}{n!(n+1)^{1/2}} \left(\sum_{j=1}^J \Phi_{j,q} \Delta_j \right)^n \right]^{-1} = 0, \quad (4.1)$$

where the functions $\Phi_{j,q}$ are constructed from the shape-functions of the elements of the nodes j found along ray path q to the target (node i). Solutions to eq. 4.1 show the expected concentration of the most saturated nodes to the outside of the model, and the least saturated nodes towards the centre. The q th ray path has a facet area a_q at a distance s_q from the target.

Once nodal solutions have been computed, formal solutions can be calculated for the brightnesses of rays along lines of sight to an observer’s position. These can be converted to maps that show the expected decrease in the observed size of the cloud with increasing amplification and saturation, for example Alcock & Ross (1985).

It is possible to investigate maser variability by simulating rotation of the cloud depicted in Fig. 2. The simulation was performed by computing the radiation transfer solution in the frame of the cloud, which can have no internal velocity gradients assuming that it rotates as a solid body. An external observer then sees the cloud with a Doppler correction that appears mostly as broadening with a small shift in the peak frequency of the maser line. The plane perpendicular to the rotation axis was chosen so as to present the longest axis of the domain periodically to the observer.

Variability of Class 2 methanol masers has been investigated in detail by Goedhart, Gaylard & van der Walt (2004), where light curves of several years duration are plotted for a variety of sources that show patterns that include monotonic growth and decay and periodic and aperiodic low-amplitude flaring. We show our light curve in Fig. 3 (left panel), while the observer’s view of the cloud at ten different times (a simulated VLBI map) is shown in the right-hand panel. The model maser has a light curve, in terms of the brightest specific intensity, that varies by a factor of ~ 3 over one rotation. The

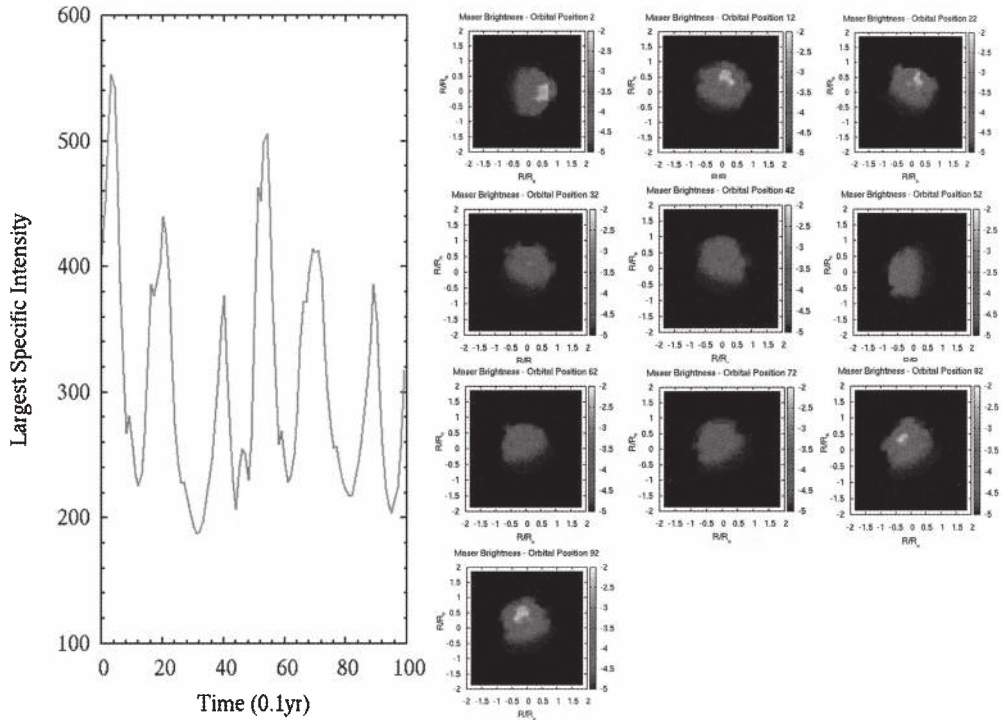


Figure 3. Left panel: The light curve of the rotating model maser in terms of the peak specific intensity (in multiples of the saturation intensity). Right panel: Snap-shots of the brightness map at various times during the cycle. A lower-depth model has been used so that the whole cloud is easily visible.

simulated map (right-hand panel) shows that the position of brightest emission also varies considerably with time.

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