

## Author Index

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Of making many books there is no end, and much study wearies the body.  
 Now all has been heard; here is the conclusion of the matter: Fear God and  
 keep his commandments, for this is the duty of all mankind.

– Ecclesiastes 12:12b-13

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