# **Unsteady Flow in Open Channels**

From river floods and tides, to systems for drainage and distribution of water, flows in open channels affect the daily lives of many people. Practitioners in water engineering rely on a thorough understanding of these flows in order to safeguard our habitat, while at the same time sustaining the water environment.

*Unsteady Flow in Open Channels* provides a coherent approach to the analyses and modelling of various types of unsteady flow, highlighting their similarities and differences. It presents a unified framework, using the relative roles of inertia and resistance to classify the different types of unsteady flow in environmental water systems. The link between analytical approaches and numerical modelling is emphasized – in particular, demonstrating how high-level computer languages, such as Python, can be used to solve advanced problems.

Every major topic in the book is accompanied by worked examples illustrating the theoretical concepts. Practical examples, showcasing inspiring research and engineering applications from the past and present, provide insight into how the theory developed. The book is also supplemented by a range of online resources, available at www.cambridge.org/battjes, including problem sets and computer codes. A solutions manual is also available for instructors. This book is intended for students and professionals working in the field of environmental water systems, in areas such as coasts, rivers, harbours, drainage, and irrigation canals.

**Jurjen Battjes** is Emeritus Professor at Delft University of Technology. Now retired, Professor Battjes had a long career in university teaching and research in the field of fluid mechanics. He taught courses in modelling, introductory fluid mechanics, unsteady flow in open channels and wind-generated waves, the latter being his major research topic. He has also been active as a consultant on numerous projects in coastal engineering, including the Deltaworks in The Netherlands. Professor Battjes has received several prizes and awards, including the International Coastal Engineering Award of the American Society of Civil Engineers.

**Robert Jan Labeur** is Assistant Professor at Delft University of Technology. He teaches various courses in environmental fluid mechanics. His research involves numerical modelling of environmental flows, water-borne transport processes and morphology, in particular the modelling of complex three-dimensional flows. Before working at the university, he was a consultant in the field of hydraulic and coastal engineering.

# **Unsteady Flow in Open Channels**

JURJEN BATTJES

**ROBERT JAN LABEUR** 





University Printing House, Cambridge CB2 8BS, United Kingdom

One Liberty Plaza, 20th Floor, New York, NY 10006, USA

477 Williamstown Road, Port Melbourne, VIC 3207, Australia

314-321, 3rd Floor, Plot 3, Splendor Forum, Jasola District Centre, New Delhi - 110025, India

79 Anson Road, #06-04/06, Singapore 079906

Cambridge University Press is part of the University of Cambridge.

It furthers the University's mission by disseminating knowledge in the pursuit of education, learning and research at the highest international levels of excellence.

www.cambridge.org Information on this title: www.cambridge.org/9781107150294 10.1017/9781316576878

© Jurjen A. Battjes and Robert Jan Labeur 2017

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 2017

A catalogue record for this publication is available from the British Library

Library of Congress Cataloging in Publication data Names: Battjes, J. A. (Jurjen Anno), 1939– author. | Labeur, R. J. (Robert Jan), 1964–author. Title: Unsteady flow in open channels / Jurjen Battjes and Robert Jan Labeur. Description: Cambridge, United Kingdom ; New York, NY : Cambridge University Press, 2017. | Includes bibliographical references and index. Identifiers: LCCN 2016035538 | ISBN 9781107150294 (Hardback ; alk. paper) | ISBN 1107150299 (Hardback ; alk. paper) Subjects: LCSH: Unsteady flow (Fluid dynamics)–Mathematical models. | Open-channel flow–Mathematical models. | Water waves–Mathematical models. | Wave equation. | Fluid mechanics–Mathematical models. Classification: LCC TA357.5.U57 B38 2017 | DDC 532/.053–dc23 LC record available at https://lccn.loc.gov/2016035538 ISBN 978-1-107-15029-4 Hardback Additional resources for this publication at www.cambridge.org/battjes

> Cambridge University Press has no responsibility for the persistence or accuracy of URLs for external or third-party internet websites referred to in this publication, and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.

# Contents

Li	st of S	Symbols		<i>page</i> xi
Pr	reface			XV
1	Basi	c Equatio	ons for Long Waves	1
	1.1	Appro	bach	1
	1.2	Schen	natization of the Cross Section	2
	1.3	Mass	Balance	3
	1.4	Equat	ions of Motion	5
		1.4.1	Euler Equations	6
		1.4.2	Flow Resistance	8
		1.4.3	Momentum Balance	10
	1.5	Sumn	nary of the Long-Wave Equations	11
	Prob	olems		12
2	Class	ification	13	
	2.1	Types	of Long Waves	13
		2.1.1	Translatory Waves	13
		2.1.2	Tsunamis	14
		2.1.3	Seiches	16
		2.1.4	Tides	17
		2.1.5	Flood Waves in Rivers	18
	2.2	A Cor	ndition for the Long-Wave Approximation	19
	2.3	Estim	ation of Terms	21
		2.3.1	Advective Acceleration Term	21
		2.3.2	Resistance Term	23
	2.4	Soluti	on Methods	24
		2.4.1	Complete Equations	24
		2.4.2	Simplified Equations	25
	Prob	olems		26
3	Elem	nentary \	Nave Equation	27
	3.1	Simpl	27	
		3.1.1	Propagation	27
		3.1.2	Balance Equations	28
	3.2	Eleme	entary Wave Equation	31
		3.2.1	Derivation	31

۷

vi		Contents		
		3.2.2 General Solution	3	
		3.2.2 Total Derivative	3	
		3.3 Relation between Discharge and Free-Surface Elevation in a Progressive	5	
		Wave	3	
		3.4 Solution for Arbitrary Initial Conditions	2	
		3.5 Boundary Conditions	1	
		3.6 Periodic Progressive and Standing Waves	2	
		3.6.1 Infinitely Long Canal		
		3.6.2 Semi-Infinitely Long Canal with a Closed End		
		3.6.3 Closed Basin	1	
		3.6.4 Semi-Closed Basin Connected to a Reservoir or Tideless Sea	2	
		3.6.5 Semi-Closed Basin Connected to a Tidal Sea	4	
		Problems		
	4	Translatory Waves	4	
		4.1 Introduction		
		4.2 Low Translatory Waves in Uniform Channels		
		4.3 Propagation in Non-Uniform Canals		
		4.3.1 Rapidly Varying Cross Section		
		4.3.2 Gradually Varying Cross Section		
		4.4 Damping of Translatory Waves		
		4.5 High Translatory Waves		
		4.5.1 Wave Deformation		
		4.5.2 Tidal Bores		
		4.5.3 Bore Propagation		
		4.6 Field Observations		
		4.6.1 Observations in the Twenthekanaal		
		4.6.2 Observations in the Approach Canal to the Lanaye Lock		
		Problems		
	5	Method of Characteristics		
		5.1 Introduction		
		5.2 Mathematical Formulation		
		5.3 Principle of Application		
		5.3.1 General Procedure		
		5.3.2 Characteristics		
		5.3.3 Boundary Conditions		
		5.3.4 External Forces		
		5.4 Graphical Solution Procedure		
		5.4.1 Initial Value Problem	,	
		5.4.2 Inclusion of the Boundary Conditions		
		5.5 Simple Wave	:	
		5.5.1 General Solution	8	

vii		Contents			
		5.5.2 Expansion Wave	85		
		5.5.3 Compression Wave	86		
		Problems	88		
	6	Tidal Basins	91		
		6.1 Introduction	91		
		6.2 Mathematical Formulation	92		
		6.2.1 Motion in the Basin	92		
		6.2.2 Motion in the Channel	93		
		6.2.3 Coupled System	96		
		6.3 Linearization of the Quadratic Resistance	98		
		6.4 System with Discrete Storage and Resistance	101		
		6.4.1 Governing Equation	101		
		6.4.2 Nonhomogeneous Solution	101		
		6.4.3 Explicit Solution	102		
		6.5 System with Discrete Storage, Resistance and Inertia	105		
		6.6 Solution through Complex Algebra	109		
		6.6.1 Complex Representation	109		
		6.6.2 Solution	110		
		Problems	111		
	7	Harmonic Wave Propagation	113		
		7.1 Introduction	113		
		7.2 Complex Representation of Damped Progressive Harmonic Waves	114		
		7.3 Formulation and General Solution	116		
		7.3.1 Formulation	116		
		7.3.2 General Solution	117		
		7.3.3 Solution of the Dispersion Equation	118		
		7.3.4 Solution for the Discharge	119		
		7.4 Unidirectional Propagation	121		
		7.4.1 Physical Interpretation	122		
		7.4.2 Propagation in Compound Channels	124		
		7.5 Bi-directional Wave Propagation	126		
		7.5.1 Relation between the Complex Amplitudes at the Ends of a			
		Prismatic Section	126		
		7.5.2 Response Function of a Semi-Closed Prismatic Basin	129		
		7.6 Propagation in Non-Uniform Channels	131		
		7.6.1 Abrunt Channel Transition	131		
		7.6.2 Exponentially Varying Cross Section	132		
		7.7 Pronagation in Networks	132		
		7.8 Nonlinear Effects	130		
		7.0 Infilled Effects 7.8.1 Tidal Ways Deformation	139		
		7.8.2 Maan Sland of the Ered Surface	129		
		Problems	139		
		riotems	141		

viii	Contents				
	8	Flood Waves in Rivers	143		
		8.1 Introduction	143		
		8.2 Quasi-Steady Approximation	144		
		8.3 Quasi-Uniform Approximation	145		
		8.3.1 Formulation and General Solution	146		
		8.3.2 The High-Water Wave Speed	146		
		8.3.3 Kinematic Wave Behaviour	147		
		8.4 Influence of Variable Free-Surface Slope	148		
		8.4.1 Diffusion Model for Flood Waves	149		
		8.4.2 Elementary Solution	151		
		8.4.3 Observations	152		
		8.5 Discussion	153		
		Problems	154		
	9	Steady Flow	157		
		9.1 Rapidly Varying Flow	157		
		9.1.1 Scaling Analysis	157		
		9.1.2 Flow Patterns	158		
		9.1.3 Bernoulli Equation	161		
		9.1.4 Relations between Water Level and Discharge	161		
		9.1.5 Hydraulic Jump	167		
		9.2 Gradually Varying Flow	168		
		9.2.1 Governing Differential Equation	168		
		9.2.2 Integral Curves	169		
		9.2.3 Classification of Backwater Curves	171		
		9.2.4 Boundary Conditions	172		
		9.2.5 Explicit Representation	172		
		9.3 Uniform Flow	176		
		9.3.1 Equilibrium Relations	176		
		9.3.2 Resistance Relations	177		
		9.3.3 The Overall Resistance of a Channel	181		
		9.3.4 Applicability to Unsteady Flow	182		
		Problems	182		
	10	Transport Processes	185		
		10.1 Introduction	185		
		10.2 Generic Balance Equation	186		
		10.3 Molecular Diffusion	187		
		10.3.1 Fick's Law of Diffusion	188		
		10.3.2 One-Dimensional Diffusion	188		
		10.3.3 The Random Walk Model	192		
		10.3.4 Two-Dimensional Diffusion	194		
		10.4 Advection and Molecular Diffusion	194		
		10.5 Turbulent Diffusion	196		

ix	Contents			
	10.5.1 Reynolds Averaging	196		
	10.5.2 Closure Hypothesis	190		
	10.6 Vertical Diffusion in Free-Surface Flows	198		
	10.6 1 Turbulence Diffusivity	198		
	10.6.2 Vertical Distribution of Horizontal Velocity	190		
	10.7 Horizontal Transport in Free-Surface Flows	200		
	10.7.1 Introduction	200		
	10.7.2 Two-Dimensional Horizontal Transport	201		
	10.7.3 One-Dimensional Horizontal Transport	207		
	Problems	210		
11	Numerical Computation of Solutions	211		
	11.1 Introduction	211		
	11.2 Canal-Basin System	212		
	11.2.1 Model Equations	212		
	11.2.2 Discretization	213		
	11.2.3 Semi-implicit Method	213		
	11.2.4 Some Other Solution Methods	215		
	11.2.5 Properties of the Semi-implicit Method	216		
	11.2.6 Python Implementation	218		
	11.2.7 Verification	220		
	11.3 Semi-Implicit Method for Long Waves	223		
	11.3.1 Model Equations	223		
	11.3.2 Discretization	224		
	11.3.3 Semi-Implicit Method	225		
	11.3.4 Some Other Solution Methods	229		
	11.3.5 Properties of the Semi-Implicit Method	232		
	11.3.6 Python Implementation	235		
	11.3.7 Verification	238		
	11.4 Characteristics-Based Methods	241		
	11.4.1 Characteristic Equations	241		
	11.4.2 Space-Time Discretization	242		
	11.4.3 Forward Time Backward Space Method	243		
	11.4.4 Some Other Characteristics-Based Methods	247		
	11.4.5 Properties	250		
	11.4.6 Python Implementation	252		
	Problems	254 256		
Λ.	nnandiy A Pressurized Flow in Closed Conduits	250		
А	A 1 Introduction	239		
	A 2 Governing Equations	239		
	A 2.1 Constitutive Faultions	200		
	A 2.2. Conservation of Mass	200		
	A.2.2 CONSERVATION OF WIASS	∠0∠		

x	Contents	
	A.2.3 Conservation of Momentum	263
	A.3 Pressure Waves in Pipelines	263
	A.3.1 Characteristic Equations	263
	A.3.2 Physical Behaviour	264
	A.4 Closure Procedures	265
	A.4.1 Abrupt Closure	265
	A.4.2 Gradual Closure	266
	A.4.3 Influence of Exit Losses and/or Wall Friction	269
	A.4.4 Influence of Time Scales	269
	Problems	270
	Appendix B Summary of Formulas	271
	References	279
	Author Index	283
	Subject Index	285

# List of Symbols

# **Roman Symbols**

- *a* acceleration of fluid particle (Chapter 2)
- *a* height of sharp-crested weir above upstream bed level (Chapter 9)
- *a* height of opening under a gate (Chapter 9)
- *A* area of entire wetted cross section
- $A_c$  area of wetted conveyance cross section
- *b* binormal coordinate
- *B* width of the free surface
- $B_c$  width of the free surface of the conveyance cross section
- c velocity of propagation of a disturbance relative to the fluid ahead of it
- c concentration of dissolved or suspended matter (Chapter 10)
- $c_D$  wind drag coefficient
- $c_f$  boundary resistance coefficient
- $c_{HW}$  velocity of propagation of a flood wave
- C Chézy coefficient
- d cross-sectionally averaged depth of conveyance cross section  $(d = A_c/B_c)$
- $d_{cr}$  critical depth
- D grain or stone diameter (Chapter 9)
- *D* inner pipe diameter (Appendix A)
- *E* energy level above local bed elevation (Chapter 9)
- *E* Young's modulus of elasticity of pipe wall material (Appendix A)
- F energy flux
- Fr Froude number
- $F_r$  resistance force
- g acceleration of gravity
- *h* elevation of the free surface above reference plane
- $h_p$  piezometric level above reference plane
- H energy level above reference plane
- *i* imaginary unit
- $i_b$  bed slope
- $i_f$  friction slope

xi

xii		List of Symbols
		slope of free surface
	k	wave number in harmonic wave or oscillation ( $k = 2\pi/L$ ) (Chapters 3 and 7)
	k	Nikuradse sand grain diameter (Chapter 9)
	K	diffusivity in flood wayes (Chapter 8)
	K	diffusivity in transport of matter (Chapter 10)
	K	modulus of compressibility of water (Appendix A)
	l	length of basin
	L	wave length
	Ĺ	length scale of the motion
	~ m	discharge coefficient
	n	Manning's n
	n	fluid pressure
	P n	complex root of dispersion equation $(n = \mu + ik)$ (Chapter 7)
	P Datas	atmospheric pressure at the air-water interface
	Paum P	wetted perimeter of conveyance cross section
	P	complex propagation constant in harmonic wave propagation (Chapter 7)
	a	discharge per unit width ( $a = O/B_{-}$ )
	q	discharge per unit what $(q = g/B_c)$
	e r	radius of curvature of a streamline (Chapter 1)
	r	ratio of wave heights at abrunt channel transition (Chanters 4 and 7)
	r	amplitude response factor (Chapters 6 and 7)
	, R	hydraulic radius $(R - A/P)$
	$R^{\pm}$	Riemann invariants
	r r	streamwise coordinate
	S	relayation length in theory of damping of translatory waves
	t S	time
	r T	wave period
	$\vec{T}$	three-dimensional transport vector
	$\tau$	time scale of the motion
	, 11	local particle velocity
	и 11.	shear velocity
	<i>u</i> * <i>I</i> /	cross-sectionally averaged streamwise particle velocity u
	14	velocity scale of the motion
	V	velocity of propagation relative to the bed $(V = U + c)$
	W	total head loss in inlet-bay system
	W10	wind speed (10-minute average at 10 m above mean water level)
	x	horizontal cartesian coordinate
	v	horizontal cartesian coordinate
	, 7	vertical cartesian coordinate, positive upward
	- 7	complex auxiliary length representing the discharge in harmonic wave propagat

xiii List of Symbols **Greek Symbols** velocity distribution coefficient in momentum flux (Chapter 1) α dimensionless parameter of the free-surface profile of a translatory wave (Chapter 4) α α arbitrary phase angle angle of bed elevation with respect to the horizontal (Chapter 1) β velocity distribution coefficient in energy flux (Chapter 9) β β arbitrary phase angle ratio of Bc-values at abrupt transition γ Г dimensionless parameter in tidal inlet-bay system δ resistance angle in propagation of harmonic waves (Chapter 7) δ wall thickness (Appendix A) infinitesimal dimensionless quantity  $\epsilon$ molecular diffusivity (Chapter 10)  $\epsilon$ turbulence diffusivity (Chapter 10)  $\epsilon_t$ surface elevation above mean water level ζ dimensionless value of  $\zeta$ η phase lag of bay tide behind exterior tide θ resistance factor with dimension 1/time in harmonic wave propagation (Chapter 7) κ Von Karman constant in theory of turbulent boundary layers (Chapter 10) κ damping modulus in harmonic wave propagation (Chapter 7) μ contraction coefficient (Chapter 9) μ kinematic turbulence viscosity  $v_t$ head loss coefficient ξ water density ρ air density  $\rho_a$ dimensionless resistance factor in harmonic wave propagation (Chapter 7) σ streamwise standard deviation of surface elevation in flood waves (Chapter 8) σ standard deviation of concentration of transported substance (Chapter 10) σ Courant number (Chapter 11) σ Φ Gaussian probability density function relaxation time in inlet-bay system τ boundary shear stress  $\tau_b$ wind shear stress at the free surface  $\tau_s$ coefficient for expansion loss and boundary resistance in inlet-bay system χ Ψ angle between wind direction and flow direction radial frequency in harmonic motion ( $\omega = 2\pi/T$ ) (0)natural (Helmholtz) frequency of inlet-bay system  $\omega_0$ 

xiv	List of Symbols		
			Diacritical Marks
	<b>(</b> 0 i 0 i 0	circumflex tilde macron	(real) amplitude of a quantity complex amplitude of a quantity (turbulence) quantity averaged over time or space

 $\circ'$ (turbulent) fluctuation of a quantity prime

- $\circ'$ prime first derivative of a function  $\circ^{\prime\prime}$ 
  - double prime second derivative of a function

# Sub- and Superscripts

subscript s	refers to sea
subscript b	refers to basin or bay or bed
subscript c	refers to conveyance (area or width)
subscript 0	refers to an initial or undisturbed flow state
subscript 0	refers to quantities of a harmonic wave in the absence of resistance
subscript cr	refers to critical flow
subscript u	refers to uniform flow
superscript +	refers to propagation in positive s-direction
superscript -	refers to propagation in negative s-direction

# Preface

This book grew out of lectures on unsteady flow in open channels in the Civil Engineering Department of the Delft University of Technology for senior BSc students and first-year MSc students in hydraulic and coastal engineering, water resources management, hydrology and sanitary engineering. It deals with gradually varying, unsteady flows, or long waves, in natural channels such as rivers, estuaries and tidal channels, as well as man-made canals for various purposes such as drainage and irrigation systems and shipping.

Most existing books on open channel flow deal mainly with steady flows, unsteady flows typically being diverted to a single chapter. In practice, unsteady flows are the rule rather than the exception. Therefore, a unified introduction was deemed necessary, in which the unsteadiness and the important associated notion of wave propagation are essential ingredients from the start. The intended readership consists of students in the above-mentioned disciplines as well as practitioners.

## Subject

The subject of this book is the mathematical modelling of gradually varying unsteady flows, or long waves, in open channels. Various classes of long waves are distinguished, depending on their origin and the associated time scale, varying from the relatively rapid translatory waves to the sluggish flood waves in lowland rivers. A chapter on steady flow summarizes some relevant results within this subclass. Transport of dissolved or suspended matter in open channels is briefly dealt with as well. Lastly, the numerical modelling of flow in conduits is covered in a separate chapter.

Pressurized flow in pipelines falls formally outside the scope of this book, but it is included nonetheless because pipe flow often is an integral part of water transport systems, and the mathematical equations describing pressurized flow and those describing open channel flow are quite similar. For these reasons, a summary is presented in Appendix A.

#### Aim

This book offers a unified presentation of the mathematical modelling of various classes of unsteady flows that can be expected in the context of design and operation of

XV

© in this web service Cambridge University Press

xvi Preface

hydraulic engineering works in tidal areas, estuaries, rivers, canals etc., e.g. dredging or the construction and operation of control structures or dams. The engineer should be able to foresee consequences of the works being designed, both qualitatively and quantitatively. This requires insight into these flows and the ability to schematize them, quantify them through mathematical modelling and computations and interpret the results. The achievement of these objectives is the primary aim of this book.

In view of the above, the more specific aims of this book can be summarized as follows:

- to provide qualitative knowledge of various classes of unsteady flow phenomena in open channels that are important in engineering practice
- to provide insight into the relative importance of various mechanisms in the dynamics of these flows
- to explain the physics of shallow-water wave propagation
- to stimulate an attitude of making a (qualitative) problem analysis including the estimation of relevant effects
- to offer a unified, systematic overview of mathematical approximations and solution methods suited to various categories of open channel flow
- to enable the reader to develop the ability to make schematizations and to perform approximative computations for the flow phenomena considered
- to develop the ability to code algorithms for the computation of unsteady open-channel flows

## Approach

A key characteristic of this book is its emphasis on the development of physical insight. This is approached through the presentation of simplified models of the principal classes of flow considered and the corresponding analytical solutions, since these show explicitly the effects of the major parameters involved.

Following the derivation of the basic one-dimensional equations for long waves (the socalled shallow-water equations), distinct classes of waves are presented and discussed. For each of these, order-of-magnitude relations between the different physical processes are derived, including the boundary resistance relative to the inertia. In fact, the latter ratio is used as the ordering principle for the remainder of the book, the successive chapters dealing with a class of flows of increasing relative resistance, going from translatory waves with negligible resistance to friction-dominated flood waves in lowland rivers.

In each of these chapters, the presentation proceeds from a qualitative discussion, via the introduction of appropriate simplifications of the momentum equation, to the development of a quantitative mathematical model. Analytical solutions are presented because these are optimally suited to the development of physical insight. The aim in these chapters is not to develop models of high quantitative accuracy. This is done in a final chapter, exclusively devoted to numerical modelling.

xvii

Preface

In view of its importance, understanding of the notion of wave propagation is developed gradually. A qualitative description of the propagation of low frictionless translatory waves in prismatic conduits prepares the way to the derivation of the corresponding general linear wave equation. Subsequently, these restrictions are gradually relaxed by considering variations in channel cross section, allowing finite wave heights, and incorporating friction. The method of characteristics is introduced next to provide added understanding as well as a formal mathematical framework for quantitative evaluations.

The practical relevance of the developed concepts is demonstrated with examples from inspiring engineering cases (such as the enclosure of the previous Zuiderzee in The Netherlands) and captivating natural phenomena (e.g. tidal bores). Field observations and some laboratory data are presented for a quantitative comparison with the theory.

Worked-out examples are presented for purposes of illustration, to provide more understanding and to aid in the ability to apply the theory. Each chapter ends with a set of Problems.

#### Layout

Chapter 1 opens with a brief description of the approach to the mathematical modelling of unsteady flow in open channels. This is followed by a presentation of the basic equations for these flows, which are the starting point for the analysis and modelling of various categories of long waves in the following chapters. Chapter 2 describes several characteristic long-wave phenomena qualitatively and presents a quantitative analysis of their major characteristics, making visible which processes are dominant and which ones are relatively weak in the various categories of long waves.

The notion of wave propagation with neglect of the effects of resistance is developed in Chapters 3 and 4, followed by the introduction of the powerful method of characteristics in Chapter 5.

Chapters 6–8 present suitable mathematical approximations for several classes of long waves. Corresponding solution techniques and solutions are presented as well. Harmonic motions are considered in Chapter 6 for standing oscillations in basins and in Chapter 7 for propagation with friction, mainly aimed at tidal propagation, in which resistance is important but not dominant. Flood waves in lowland rivers, in which inertial effects can be neglected relative to resistance, are the subject of Chapter 8.

Chapter 9 gives a brief summary of the modelling of steady flows, again in the order of increasing slowness, viz. rapidly varying steady flow through control structures, gradually varying steady flows (backwater curves) and finally uniform flow, which in essence is a summary of expressions for boundary resistance. Chapter 10 presents an introduction to the modelling of transport processes. Principles of numerical modelling of unsteady flows in open channels are dealt with in Chapter 11.

Lastly, Appendix A covers pressurized flow in pipes. A summary of equations is presented in Appendix B.

xviii

Preface

## **Prior Knowledge**

The treatment of the various subjects relies on prior knowledge of basic fluid mechanics and an understanding of ordinary and partial differential equations and complex algebra.

Awareness of civil engineering will help in the understanding of the book, but this is not considered essential. The book includes some worked examples using simple computer code (written in Python) for which basic programming skills will be useful. These may also be learned, however, by following along with the examples.

### **Course Plan**

Teaching all of the material covered in the book will take some 24–36 lectures of  $1\frac{1}{2}$  teaching hours each, depending on the depth at which the various topics are treated and the expected self-study effort. When scheduled during a full semester, the course will typically take two lectures per week, while an additional 3–4 hours will be required weekly for self-study. Including exam preparation (2 days), the total work load for the student will amount to about 170 hours.

Chapters 1–8 are considered the backbone of the course. Related topics are dealt with in Chapters 9–11. The latter are often part of other, more dedicated, courses, in which case they can be omitted from the course plan. This will reduce the total working load to about 120 hours. The reduced course would also fit nicely into a half-semester schedule consisting of three lectures a week and 5–6 hours of self-study.

For self-study rehearsal every chapter concludes with a series of Problems for which a solutions manual is available separately. General solution strategies are explained in the worked examples preceding each Problems section. A series of digital exercises is available for the reader to become familiar with the concepts of the corresponding topic and to practise, progressively, the required skills. They also include so-called diagnostic tests, to assess one's preparedness for the exam.

#### Literature

The mathematical models for the considered long-wave categories presented in this book are classical (with a few exceptions for an extension of the theory). Thus, no references are made to individual contributors. Instead, we refer to the textbooks on the subject listed below, to which we are much indebted. Only in cases of very specific results, and in cases where results bear the name of the originator, have individual references been given.

Chaudry, M. H. 1993. Open-Channel Flow. Prentice Hall.

French, R. H. 1985. Open-Channel Hydraulics. McGraw-Hill.

xix

Preface

Henderson, F. M. 1966. *Open Channel Flow*. Macmillan.Sturm, T. W. 2010. *Open Channel Hydraulics*. McGraw-Hill.Ven Te Chow 1959. *Open-Channel Hydraulics*. McGraw-Hill.

# **Supplementary Materials**

The book comes with a collection of supplementary materials, which is available online. Included are a solutions manual for the Problems at the end of each chapter, a series of digital tests (for use in a MapleTA environment), and some Python scripts for carrying out the computations and Problems of Chapter 11.

# Acknowledgements

The authors thank the reviewers of the proposal for this book, as well as the editors at Cambridge University Press, for their helpful suggestions. Professor Ad Reniers and Dr. Marcel Zijlema are gratefully acknowledged for critically reading parts of the manuscript and for their constructive criticisms.

Jurjen Battjes Robert Jan Labeur