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978-1-107-03570-6 - How Humans Learn to Think Mathematically: Exploring the Three  
Worlds of Mathematics  
David Tall  
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# How Humans Learn to Think Mathematically

Exploring the Three Worlds  
of Mathematics

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32 Avenue of the Americas, New York, NY 10013-2473, USA

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Information on this title: [www.cambridge.org/9781107668546](http://www.cambridge.org/9781107668546)

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First published 2013

Printed in the United States of America

*A catalogue record for this publication is available from the British Library.*

*Library of Congress Cataloguing in Publication data*

Tall, David Orme.

How humans learn to think mathematically : exploring the three worlds of mathematics (embodiment, symbolism, formalism) / David Tall.

pages cm. – (Learning in doing : social, cognitive and computational perspectives)

Includes bibliographical references and index.

ISBN 978-1-107-03570-6 (hardback) – ISBN 978-1-107-66854-6 (paperback)

1. Mathematics – Philosophy. 2. Mathematics – Psychological aspects.

3. Mathematics – Study and teaching. 4. Thought and thinking.

5. Knowledge, Theory of. 6. Cognition. 7. Cognition in children. I. Title.

QA8.4.T33 2013

510.1–dc23 2013002749

ISBN 978-1-107-03570-6 Hardback

ISBN 978-1-107-66854-6 Paperback

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