

Networked Life

How does Google sell ad space and rank webpages? How does Netflix recommend movies, and Amazon rank products? How can you influence people on Facebook and Twitter, and can you really reach anyone in six steps? Why doesn't the Internet collapse under congestion, and does it have an Achilles' heel? Why are you charged per gigabyte for mobile data, and how can Skype and BitTorrent be free? How big is the "cloud" of cloud services, and why is WiFi slower at hotspots than at home?

Driven by 20 real-world questions about our networked lives, this book explores the technology behind the multi-trillion dollar Internet, wireless and online media industries. Providing easily understandable answers for the casually curious, alongside detailed explanations for those looking for in-depth discussion, this thought-provoking book is essential reading for students in engineering, science and economics, for network industry professionals, and for anyone curious about how technological and social networks really work.

Mung Chiang is a Professor of Electrical Engineering at Princeton University, and Director of the Princeton EDGE Lab. He has received the IEEE Kiyo Tomiyasu Award, and a US Presidential Early Career Award for Scientists and Engineers, for his research on networking. A co-founder and advisor to several startups, he also received a Technology Review TR35 Award for his contributions to network technology innovation. He is a fellow of the IEEE.

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“We are entering a new Internet era – the era of the likes of Google, Amazon, Netflix, and Facebook – with entirely new types of problems. This book captures the new era, taking a fresh approach to both topic coverage and pedagogic style. Often at the end of a section it leaves the reader asking questions; then exactly those questions are answered in the subsequent section. Every university should offer a course based on this book. It could be taught out of both ECE or CS departments at the undergraduate or graduate levels.”

Keith Ross, Polytechnic Institute of NYU

“How do the networks, which we increasingly rely upon in our everyday life, actually *work*? This book is an inspiring romp through the big ideas in networking, which is immediately rewarding and will motivate later courses.”

Frank Kelly, University of Cambridge

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MUNG CHIANG

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To my family

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Preface

You pick up your iPhone while waiting in line at a coffee shop. You Google a not-so-famous actor and get linked to a Wikipedia entry listing his recent movies and popular YouTube clips. You check out user reviews on IMDb and pick one, download that movie on BitTorrent or stream it in Netflix. But for some reason the WiFi logo on your phone is gone and you're on 3G. Video quality starts to degrade a little, but you don't know whether it's the video server getting crowded in the cloud or the Internet is congested somewhere. In any case, it costs you \$10 per gigabyte, and you decide to stop watching the movie, and instead multitask between sending tweets and calling your friend on Skype, while songs stream from iCloud to your phone. You're happy with the call quality, but get a little irritated when you see that you have no new followers on Twitter.

You've got a typical networked life, an online networked life.

And you might wonder how all these technologies “kind of” work, and why sometimes they don't. Just flip through the table of contents of this book. It's a mixture: some of these questions have well-defined formulations and clear answers while for others there is still a significant gap between the theoretical models and actual practice; a few don't even have widely accepted problem statements. This book is about formulating and answering these 20 questions.

This book is about the networking technologies we use each day as well as the fundamental ideas in the study of networks. Each question is selected not just for its relevance to our daily lives, but also for the core concepts and key methodologies in the field of networking that are illustrated by its answer. These concepts include aggregation and influence, distributed coordination, feedback control, and strategic equilibrium. And the analytic machineries are based on mathematical languages that people refer to as graph, optimization, game, and learning theories.

This is an undergraduate textbook for a new course created in 2011 at Princeton University: **Networks: Friends, Money, and Bytes**. The course targets primarily juniors and seniors in electrical engineering and computer science, but also beginning graduate students as well as students from mathematics, sciences, economics, and engineering in general. It can be viewed as a second course after the “signals and systems” course that anchors the undergraduate electrical and computer engineering curriculum today. Starting in September 2012, this course

is also on free open access platforms, such as Stanford's coursera and the course's own open education website, as well as on YouTube and iTunes U.

This book weaves a diverse set of topics you would not normally see under the same cover into a coherent stream: from Arrow's impossibility and Rawls' fairness to Skype signaling and Clos networks, from collaborative filtering and firefly synchronization to MPEG/RTSP/TCP/IP and WiFi CSMA DCF. This begs a question: "So, what *is* the discipline of this book?" This is a question that most of the undergraduates do not care about. Neither does this book, which only wants to address these practical questions, using whatever modeling languages that have been observed to be the most relevant ones so far. It turns out that there is a small, common set of mathematics which we will need, but that's mostly because people have invented only a limited suite of modeling languages.

This is not a typical textbook for another reason. It does not start with general theories as do many books on these subjects, e.g., graph theory, game theory, and optimization theory, or with abstract concepts like feedback, coordination, and equilibrium. Instead it starts with concrete applications and practical answers, and sticks to them (almost) every step of the way. Theories and generalizations emerge, as if they were "accidental by-products," during the process of formulating and answering these questions.

This book can be supplemented with its website: <http://www.network20q.com>, including lecture slides, problem solutions, additional questions, examples of advanced material, further pointers to references, collections of news media coverage of the topics, "currency-earning" activities, course projects, blogs, tweets, surveys, and student-generated course material in wiki. We have created web features that turn this class into an online social network and a "networked economy."

This book can also be used by engineers, technology managers, and pretty much anyone with a keen interest in understanding how social and technological networks work. Often we sacrifice generality for accessibility, and supplement symbolic representation with numerical illustration.

- The first section of each chapter is a "short answer," and it is accessible by most people.
- Then there's a "long answer" section. If you remember differentiation and linear algebra (and occasionally a little bit of integration and basic probability), you can follow all the material there. We try to include only those symbols and equations that are really necessary to unambiguously express the ideas.
- The "examples" section contains detailed, numerical examples to reinforce the learning from the "long answer" section. On average, these first three sections of each chapter form the basis of one 80-minute lecture. Several of these lectures will go over 80 minutes while several others, including the last two, can be covered under 80 minutes.

- Each chapter concludes with a section on “advanced material,” which requires the reader to be quite comfortable with symbolic operations and abstract reasoning, but can be skipped without losing the coherence and gist of the book. In the undergraduate course taught at Princeton, hardly any of the advanced material is covered. Covering all the “advanced material” sections would constitute an introductory graduate-level course. To keep the book thin, worked examples for these sections are pushed to the course website.
- At the end of each chapter, there are five homework questions, including easy drills, essential supplements, and some “out-of-syllabus” explorations about networks in biology, energy, magic, music, and transportation. The level of difficulty is indicated on a scale of one (easy) to three (hard) stars. On the course website, there is a much larger collection of additional homework problems, including many multiple-choice questions testing the basic understanding of the material.
- There are also five key references per chapter (yes, only five, in the hope that undergraduates may actually read some of these five, and my apologies to the authors of thousands of papers and books that could have been cited). These references open the door to further reading, including textbooks, research monographs, and survey articles.

This is a (relatively) thin book. It’s a collage of snapshots, not an encyclopedia. It’s an appetizer, not an entree. The majority of readers will not pursue a career specializing in the technical material in this book, so I take every opportunity to delete material that’s very interesting to researchers but not essential to this undergraduate course. Each one of these 20 chapters deserves many books for a detailed treatment. I only highlight a few key ideas in the span of about 20 pages per chapter and 80 minutes per lecture. There are also many other mathematical languages in the study of networks, many other questions about a networked life, and many other types of networks that we do not have time to cover in one semester. But as the saying goes for a course: “It’s more important to *uncover* than to cover a lot.”

This is a book illustrating some pretty big ideas in networking, through 20 questions we can all relate to in our daily lives. Questions that tickle our imagination with surprises and incomplete answers. Questions that I wished I had known how to answer several years ago. Questions that are quickly becoming an essential part of modern education in electrical and computer engineering.

But above all, I hope this book is fun to read.

Mung Chiang
Princeton, NJ
July 2012

Acknowledgements

In so many ways I've been enjoying the process of writing this book and creating the new undergraduate course at Princeton University. The best part is that I got to, ironically in light of the content of this book, stay *offline* and focus on learning a few hours a day for several hundred days. I got to digest wonderful books and papers that I didn't have a chance to read before, to think about the essential points and simple structures behind the drowning sea of knowledge in my research fields, and to edit and re-edit each sentence I put down on paper. It reminded me of my own sophomore year at Stanford University one and a half decades ago. I often biked to the surreally beautiful Oval in the morning and dived into books of many kinds, most of which were not remotely related to my majors. As the saying goes, that was a pretty good approximation of paradise.

That paradise usually ends together with the college years. So I have many people to thank for granting me a precious opportunity to indulge myself again at this much later stage in life.

- The new course “Networks: Friends, Money, and Bytes” could not have been created in 2011 without the dedication of its three remarkable TAs: Ji-asi Chen, Felix Wong, and Pei-yuan Wu. They did so much more for the course than a “normal” TA experience: creating examples and homework problems, initiating class activities, and running the online forum.
- Many students and postdocs in Princeton's EDGE Lab and EE Department worked with me in creating worked examples and proofreading the drafts: Chris Brinton, Amitabha Ghosh, Sangtae Ha, Joe Jiang, Carlee Joe-Wong, Yiannis Kamitsos, Haris Kremo, Chris Leberknight, Srinivas Narayana, Soumya Sen, Victoria Solomon, Arvid Wang, and Michael Wang.
- Princeton students in ELE/COS 381's first offering were brave enough to take a completely new course and contributed in many ways, not the least through the class website blogs and course projects. Students in the graduate course ELE539A also helped proofread the book draft and created multiple choice questions.
- Before I even got a chance to advertise the course, some colleagues already started planning to offer this course at their institutions in 2012: Jianwei Huang (Chinese University of Hong Kong), Hongseok Kim (Sogang University, Korea), Tian Lan (George Washington University), Walid Saad

(University of Miami), Chee Wei Tan (City University of Hong Kong), and Kevin Tang (Cornell University).

- The material in this book is inspired by discussions with colleagues in both academia and industry over the years. Since last summer, more than fifty colleagues has provided valuable suggestions directly for the course and the book. In particular, I received very detailed comments on earlier drafts of the book from Keith Cambron (AT&T Labs), Kaiser Fung (Sirius), Victor Glass (NECA), Jason Li (IAI), Jennifer Rexford (Princeton), Keith Ross (NYU Poly), Krishan Sabnani (Bell Labs), Walid Saad (University of Miami), Matthew Salganik (Princeton), Jacob Shapiro (Princeton), Kevin Tang (Cornell), and Walter Willinger (AT&T Labs), among others.
- Phil Meyler from Cambridge University Press encouraged me to turn the lecture notes into a textbook, and further connected me with a group of enthusiastic staff at CUP. I am grateful to the entire Cambridge editorial and marketing team across their UK and New York offices.
- This course was in part supported by a grant from the US National Science Foundation, in a program run by Darleen Fisher, for a team consisting of two engineers and two social scientists at Princeton. I'm glad to report that we achieved this educational goal in our proposal, and did that before the project's official end date.

My appreciation traces back to many of my teachers. For example, I've had the fortune to be co-advised in my Ph.D. study by Stephen Boyd and Tom Cover, two brilliant scholars who are also superb teachers. Their graduate-level textbooks, *Convex Optimization* by Boyd and Vandenberghe and *Elements of Information Theory* by Cover and Thomas, are two towering achievements in engineering education. Read these two books, and you'll "experience" the definition of "clarity," "accessibility," and "insight." When I was writing research papers with them, Tom would spend many iterations just to get one notation right, and Stephen would even pick out each and every LaTeX inconsistency. It was a privilege to see first-hand how the masters established the benchmarks of technical writing.

Stephen and Tom were also the most effective lecturers in classroom, as was Paul Cohen, from whom I took a math course in my sophomore year. Pulling off the sweatshirt and writing with passion on the blackboard from the first moment he entered the classroom, Paul could put your breath on hold for 80 minutes. Even better, he forgot to give us a midterm and then gave a week-long, take-home final that the whole class couldn't solve. He made himself available for office hours on-demand to talk about pretty much anything related to math. The course was supposed to be on PDE. He spent just four lectures on that, and then introduced us to eighteen different topics that quarter. I've forgotten most of what I learned in that course, but I'll always remember that learning can be so much fun.

In the same winter quarter that I took Stephen's and Tom's courses, I also took from Richard Rorty a unique course at Stanford called "From Religion through Philosophy to Literature," which pulled me out of Platonism to which I had been increasingly attached as a teenager. Talking to Rorty drastically sharpened my appreciation of the pitfalls of mistaking representations for reality. A side-benefit of that awakening was a repositioning of my philosophy of science, which propagated to the undercurrents of this book.

Three more inspirations, from those I never met:

- Out of all the biographies I've read, the shortest one, by far, is by Paul Johnson on Churchill. And it's by far the most impactful one. Brevity is power.
- But even a short book feels infinitely long to the author until it goes to the press. What prevented me from getting paralyzed by procrastination is Frederick Terman's approach of writing textbooks while leading a much busier life (serving as a Dean and then the Provost at Stanford, and creating the whole Silicon Valley model): write one page each day.
- Almost exactly one century ago, my great grandfather, together with his brother, wrote some of the first modern textbooks in China on algebra and on astronomy. (And three decades ago, my grandfather wrote a textbook on econometrics at the age of seventy.) As I was writing this book, sometimes I couldn't help but picture the days and nights that they spent writing theirs.

For some reason, the many time commitments of a professor are often hard to compress. And I couldn't afford to cut back on sleep too much, for otherwise the number of mistakes and typos in this book would have been even larger. So it's probably fair to say that each hour I spent writing this book has been an hour of family time lost. Has that been a good tradeoff? Definitely not. So I'm glad that the book is done, and I'm grateful to my family for making that happen: my parents who helped take care of my toddler daughter when I was off to dwell in this book, my wife who supported me sitting there staring at my study's ceiling despite her more important job of curing the ill, and Novia who could have played with her Daddy a lot more in the past year. This book was written with my pen and their time.

Roadmap

This roadmap is written for course instructors, or perhaps as an *epilogue* for students who have already finished reading the book, especially Figure 0.3 and the list of 20 ideas below it. It starts with a taxonomy of the book and introduces its organization and notation. Then it discusses the similarities and differences between this book and some excellent books published over the last decade. Then it highlights three pedagogical principles guiding the book: Just In Time, Bridge Theory and Practice, and Book As a Network, and two contexts: the importance of domain-specific functionalities in network science and the need for undergraduate-curriculum evolution in electrical and computer engineering. It concludes with anecdotes of arranging this course as a social and economic network itself.

Taxonomy and Organization

The target audience of this book is both students and engineering professionals. For students, the primary audience are those from engineering, science, economics, operations research, and applied mathematics, but also those on the quantitative side of sociology and psychology.

There are three ways to use this book as a textbook.

- *An undergraduate general course at sophomore or junior level:* Go through all 20 chapters without reading the Advanced Material sections. This course serves as an introduction to networks before going further into senior-level courses in four possible directions: computer networking, wireless communication, social networks, or network economics.
- *An undergraduate specialized course at senior level:* Pick either the social and economic network chapters or the technology and economic network chapters, and go through the Advanced Material sections in those chapters.
- *A first-year graduate level course:* Go through all 20 chapters, including the Advanced Material sections.

While this book consists of 20 chapters, there are just four key recurring concepts underlying this array of topics. Table 0.1 summarizes the mapping from chapter number to the concept it illustrates.

Table 0.1 Key concepts: The chapters where each of the four key concepts show up for different types of networks.

Network Type	Aggregation & Influence	Distributed Coordination	Feedback Control	Strategic Equilibrium
Wireless		1	19	
Internet		10, 13, 16	14	
Content Distribution		15, 17	18	
Web	3, 4, 5			2
Online Social	6, 8	9	7	
Internet Economics		20		11, 12

The modeling languages and analysis machineries originate from quite a few fields in applied mathematics, especially the four foundations summarized in Table 0.2.

Table 0.2 Main methodologies: The chapters where each of the four families of mathematical languages are used in different types of networks.

Network Type	Graph Theory	Optimization Theory	Game Theory	Learning Theory
Wireless		18, 19	1	
Internet	10	13, 14, 16		
Content Distribution		15, 17		
Web	3		2	4, 5
Online Social	7, 8, 9		6	
Internet Economics		11	20	12

The order of appearance of these 20 questions is arranged so that clusters of highly related topics appear next to each other. Therefore, we recommend going through the chapters in this sequence, unless you're OK with flipping back every now and then when key concepts from prior chapters are referenced. Figure 0.1 summarizes the "prerequisite" relationship among the chapters.

This book cuts across both networks among devices and networks among people. We examine networks among people that overlay on top of networks among devices, but also spend half of the book on wireless networks, content distribution networks, and the Internet itself. We'll illustrate important ideas and useful methodologies across both types of networks. We'll see striking parallels in the underlying analytic models, but also crucial differences due to domain-specific details.

We can also classify the 20 questions into three groups in terms of the stages of development in formulating and answering them:

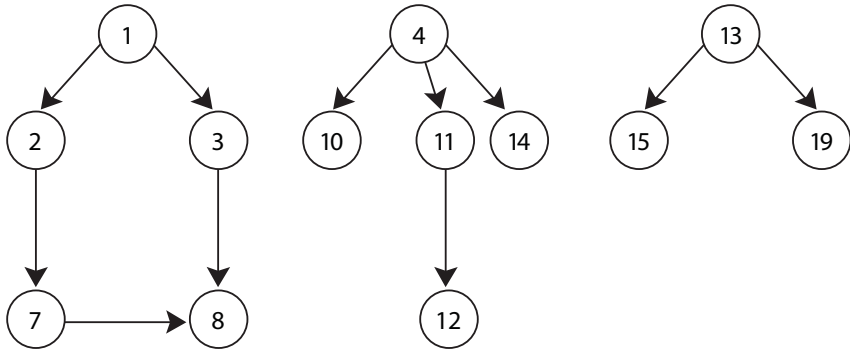


Figure 0.1 Dependence of mathematical background across some of the chapters is shown in these graphs. Each node is a chapter. Each directional link is a dependence relationship, e.g., Chapter 8’s material requires that in Chapter 3 (which in turn requires that in Chapter 1) and that in Chapter 7 (which in turn requires that in Chapter 2, which in turn requires that in Chapter 1). Chapters 1, 4, and 13, the root nodes of these three trees, offer foundational material for ten other chapters. Some chapters aren’t shown here because they don’t form part of a dependence tree.

- Question well formulated, and theory-inspired answers adopted in practice: 1, 2, 3 4, 9, 10, 11, 13 14, 15, 16, 17, 18, 19.
- Question well formulated, but there’s a gap between theory and practice (and we will discuss some possible bridges over the gaps): 12, 20.
- Question less well formulated (but certainly important to raise and explore): 5, 6, 7, 8.

It’s comforting to see that most of our 20 chapters belong to the first group. Not surprisingly, questions about technological networks tend to belong to the first group, with those about social and economic networks gravitating more towards the second and third groups. It’s often easier to model networked devices than networked human beings with predictive power.

Not all chapters explicitly study the impact of network topology, e.g., Chapter 7 studies influence models with decision externalities that are based on population sizes, while Chapter 8 looks at influence models with topology taken into account.

A quick word about the homework problems. There are five problems at the end of each chapter. These are a mixture of easy drills, simple extensions, challenging mini-research projects, and open-ended questions. Some important topics that we cannot readily fit into the main flow of the text are also postponed to the homework problem section. For those looking for more of the easy drills, the course website www.network20q.com offers additional questions.

Notation

We use **boldface** text for key terms when each is first defined. We use *italics* to highlight important, subtle, or potentially confusing points.

We use boldface math symbols to denote vectors or matrices, e.g., \mathbf{x} , \mathbf{A} . Vectors are column vectors by default. We do not use special fonts to represent sets when they are clear from the context. We use (t) to index iterations over continuous time, and $[t]$ or $[k]$ to index iterations over discrete time. We use $*$ to denote optimal or equilibrium quantities.

Some symbols have different meanings in different chapters, because they are the standard notation in different communities.

Related Books and Courses

There's no shortage of books on networks of many kinds. The popular ones that appeared in the past decade fall into two main groups:

- Popular science books, many of them filled with historical stories, empirical evidence, and sometimes a non-mathematical sketch of technical content. Some of the widely-read ones are *Bursts*, *Connected*, *Linked*, *Money Lab*, *Planet Google*, *Six Degrees*, *Sync*, *The Perfect Storm*, *The Tipping Point*, and *The Wisdom of Crowds*. Two other books, while not exactly on networks, provide important insights into many topics in networking: *Thinking, Fast and Slow* and *The Black Swan*. On the technology networks side, there are plenty of “for dummies” books, industry certification prep books, and entrepreneurship books. There are also several history-of-technology books, e.g., *Where the Geeks Stay Up Late* and *The Qualcomm Equation*.
- Popular undergraduate- or graduate-level textbooks. On the graph-theoretic and economic side of networking, three excellent textbooks appeared in 2010: *Networks, Crowds, and Markets* by Easley and Kleinberg, *Networks* by Newman, and *Social and Economic Networks* by Jackson. The last two are more on the graduate level. An earlier popular textbook is *Social Network Analysis: Methods and Applications* by Wasserman and Faust. On the computer networking side, there's a plethora of excellent textbooks. Two particularly popular ones today are *Computer Networking: A Top-Down Approach* by Kurose and Ross, and *Computer Networks: A Systems Approach* by Peterson and Davie. On wireless communications, several textbooks published in the last few years have become popular: *Wireless Communications* by Molisch, *Wireless Communications* by Goldsmith, and *Fundamentals of Wireless Communication* by Tse and Viswanath.

As illustrated in Figure 0.2, this book fills in the gap between existing groups of books.

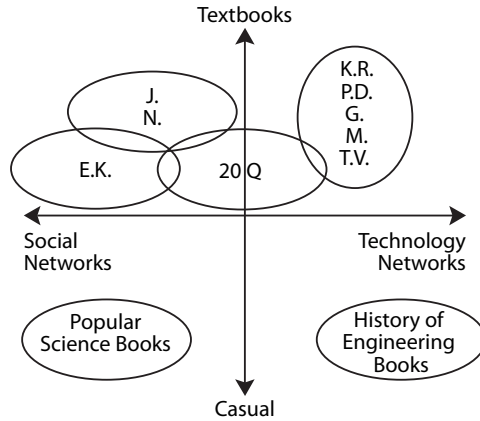


Figure 0.2 A cartoon illustrating roughly where some of the related books sit on two axes: one on the level of difficulty ranging from leisurely reading to graduate-level textbooks, and another on the mix of topics ranging from social and economic networks to technological networks. E.K. stands for Easley and Kleinberg, J. stands for Jackson, N. stands for Newman, K. R. stands for Kurose and Ross, P. D. stands for Peterson and Davie, G stands for Goldsmith, M stands for Molisch, and T.V. stands for Tse and Viswanath. 20Q stands for this book.

- Each chapter is driven by a practical question or observation, and the answers (or approximate answers) are explained using the rigorous language of mathematics. But mathematics never precedes practical problems.
- It also maintains a balance between social/economic networks and Internet/wireless networks, and between graph/economic theory and optimization/learning theory. For example, why WiFi works slower in hot spots is given as much attention as how Google auctions its ad spaces, and how IPTV networks operate is given as much detail as when information cascades initiate in a social group.
- A main goal of this book is to put social economic networks and technological networks side by side, and highlight their surprising similarities in spirit and subtle differences in detail. These examples range from the relation between Qualcomm's CDMA power control and Google's PageRank webpage ranking, to the connection between Galton's ox-weight estimation and 802.11n multiple-antenna WiFi.

These are also the differences between the Princeton undergraduate course and the seminal courses by Easley and Kleinberg at Cornell, and by Kearns at Penn. Those two courses have inspired a few similar courses at the interface between economics and computer science, such as those by Acemoglu and Ozdaglar at MIT, by Chaintreau at Columbia, by Kempe at USC, by Parkes at Harvard, by Prabhakar at Stanford, by Spielman at Yale, by Wierman at Caltech...

These excellent courses have started structuring social and economic networking topics to undergraduates. On the other hand, both computer networking and wireless communications courses are standard, indeed often required, courses at many universities' Computer Science (CS) and Electrical Engineering (EE) departments. And across the EE, CS, Economics, Operations Research, and Applied Math departments, optimization theory, game theory, learning theory, and graph theory all have their separate courses. The new course at Princeton sits in-between the CS/Econ topics and the EE topics on networks. We hope there'll be more courses in EE and CS departments around the world that use unambiguous languages to teach the concepts and methods common to social, economic, and technological networks.

Pedagogical Principles

This book and the associated course are also an experiment in three principles of teaching networks: JIT, BTP, and BAN.

Principle 1: Just In Time (JIT)

Models are often crippled by their own assumptions to start with, and frequently end up being largely irrelevant to what they set out to enable. Once in a while this is not true, but that's a low-probability event. That's why modeling is hard, especially for networks. So, before presenting any model, we first try to justify why the models are really necessary for the practical problems we face in each chapter. The material is arranged so that extensive mathematical machinery is introduced bit by bit, each bit presented just in time for the question raised. We enforce this "just-in-time" policy pretty strictly: no mathematical machinery is introduced unless it's used within the same section.

This might seem to be a rather unconventional way to write a textbook on the mathematical side of engineering. Usually a textbook asks the students to be patient with 50, 100, sometimes 200 pages of mathematics to lay the foundation first, and promises that motivating applications are coming after these pages. It's like asking a three-year-old to be patient for a long drive and promising ice-cream cones after many miles on the highway. In contrast, this book hands out an ice-cream cone every minute along the way, so that the three-year-old becomes very motivated to keep the journey going. It's more fun when gratification isn't delayed. "Fun right now" and "instant gratification" are what this book tries to achieve.

This book is an experiment motivated by this hypothesis: what professors call "fundamental knowledge" can be taught as "by-products" in the answers to practical questions that the undergraduates are interested in. A devoted sequence of lectures focusing exclusively (or predominantly) on the fundamental knowledge is not the *only* way to teach the material. Maybe we could also chop up the

material and sprinkle it around. This does not “water-down” the material, it simply reorganizes it so that it shows up right next to the applications in each and every lecture. The downside is that the standard trains of thought running through the mathematical foundation of research communities are interrupted many times. This often leaves me feeling weird because I could not finish my normal teaching sequence, but the instructor feeling uncomfortable is probably a good sign. The upside is that undergraduates, who may not even be interested in a career in this field, view the course as completely driven by practical questions.

For example, the methodologies of optimization theory are introduced bit by bit in this book: linear programming and Perron-Frobenius theory in power control, convexity and least squares in Netflix recommendation, network utility maximization in Internet pricing, dynamic programming and multi-commodity flow in Internet routing, the gradient algorithm and dual decomposition in congestion control, and combinatorial optimization in peer-to-peer networks.

The methodologies of game theory are introduced bit by bit: the basic definitions in power control, auction theory in ad-space auctions, bargaining theory in Wikipedia consensus formation as well as in two-sided pricing of Internet access, and selfish maximization in tipping.

The methodologies of graph theory are introduced bit by bit: matching in ad-space auctions, consistency and PageRank in Google search, bipartite graph in Netflix recommendation, centrality, betweenness, and clustering measures in influence models, small worlds in social search, scale-free graphs in Internet topology, the Bellman–Ford algorithm and max flow min cut in Internet routing, and tree embedding in peer-to-peer networks.

The methodologies of learning theory are introduced bit by bit: collaborative filtering in Netflix recommendation, Bayesian estimation and adaptive boosting in ratings, and community detection in influence models.

Principle 2: BTP (Bridge Theory and Practice)

The size of the global industry touched upon by these 20 questions is many trillions of dollars. Just the market capitalizations of the 20 most relevant US companies to this book: Apple, Amazon, AT&T, Cisco, Comcast, Disney, eBay, EMC, Ericsson, Facebook, Google (including YouTube), Groupon, HP, Intel, LinkedIn, Microsoft (including Skype), Netflix, Qualcomm, Verizon, and Twitter added up to over \$2.22 trillion as of July 4, 2012.

In theory, this book’s theories are directly connected to the practice in this multi-trillion-dollar industry. In practice, that’s not always true, especially in fields like networking where stable models, like the additive Gaussian noise channel for copper wire in communication theory, often do not exist.

Nonetheless, we try to strike a balance between

- presenting enough detail so that answers to these practical questions are grounded in actual practice rather than in “spherical cows” and “infinite

planes,” (although we couldn’t help but keep “rational human beings” in several chapters), and

- avoiding too much detail that reduces the “signal-noise-ratio” in illustrating the fundamental principles.

This balance is demonstrated in the level of detail with which we treat network protocol descriptions, Wikipedia policies, Netflix recommendation algorithms, etc. And this tradeoff explains the (near) absence of random graph theory and of Internet protocols’ header formats, two very popular sets of material in standard textbooks in math/CS-theory/sociology and in CS-systems/EE curricula, respectively.

Some of these 20 questions are currently trapped in particularly deep theory–practice gaps, especially those hard-to-formulate questions in Chapters 5 and 6, and those hard-to-falsify answers in Chapters 7 and 8. The network economics material in Chapters 11 and 12 also fits many of the jokes about economists, too many to quote here. (A good source of them is Taleb’s *The Bed of Procrustes*.) Reverse engineering, shown across several chapters, has its own share of accurate jokes: “Normal people look at something that works in theory, and wonder if it’ll also work in practice. Theoreticians look at something that works in practice, and wonder if it’ll also work in (their) theory.”

Time and time again, we skip the techniques of mathematical acrobats, and instead highlight the never-ending struggles between representations and realities during modeling: the process of “mathematical crystallization” where (most) parts of reality are thrown out of the window so that what remains becomes tractable using today’s analytic machineries. What often remains unclear is whether the resulting answerable questions are still relevant and the resulting tractable models still have predictive powers. However, when modeling is done “right,” engineering artifacts can be explained rather than just described, and better design can be carried out top-down rather than by “debug and tweak” It’s often been quoted (mostly by theoreticians like me) that “there’s nothing more practical than a good theory,” and that “a good theory is the first-order exponent in the Taylor expansion of reality.” Perhaps these can be interpreted as *definitions* of what constitutes a “good” theory. By such a definition, this book has traces of good theory, thanks to many researchers and practitioners who have been working hard on bridging the theory-practice gaps in networking.

Principle 3: BAN (Book As a Network)

Throughout the chapters, comparisons are constantly drawn with other chapters. This book itself is a network, a network of ideas living in nodes called chapters, and we grasp every opportunity to highlight each possible link between these nodes. The most interesting part of this book is perhaps this network effect among ideas: to see how curiously related, and yet crucially different they are.

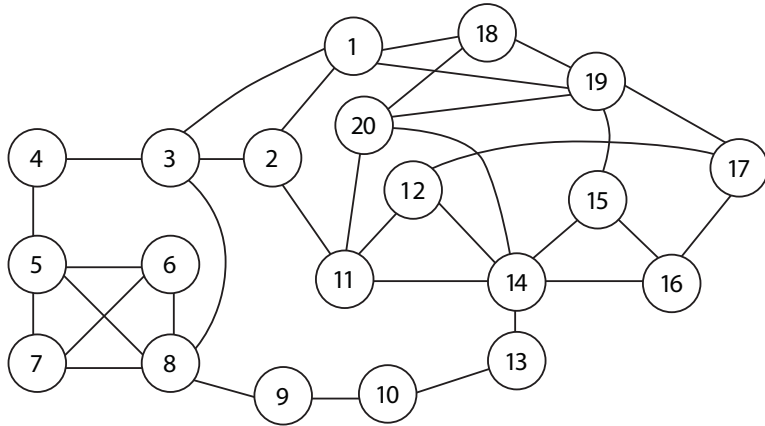


Figure 0.3 Intellectual connections across the chapters. Each node is a chapter, and each bidirectional link is an intellectual connection, via either similar concepts or common methodologies. Cliques of nodes and multiple paths from one node to another are particularly interesting to observe in this graph.

Figure 0.3 shows the main connections among the chapters. This is what the book is about: weave a network of ideas (about networks), and the positive network effect comes out of that.

We can extract the top 20 ideas across the chapters. The first 10 are features of networks, the next 5 design ideas, and the last 5 modeling approaches.

1. Resource sharing (such as statistical multiplexing and fairness): Chapters 1, 11, 13, 14, 15, 16, 17, 18, 20.
2. Opinion aggregation and consensus formation: Chapters 3, 4, 5, 6, 18.
3. Positive network effect (such as resource pooling and economy of scale): Chapters 9, 11, 13, 15, 16.
4. Negative network effect (such as tragedy of the commons): Chapters 11, 20.
5. The wisdom of crowds (diversity gain and efficiency gain): Chapters 7, 8, 18, 19.
6. The fallacy of crowds (cascade and contagion): Chapters 7, 8.
7. Functional hierarchy and layering: Chapters 13, 14, 15, 17, 19.
8. Spatial hierarchy and overlaying: Chapters 10, 13, 15, 16, 17.
9. From local actions to global property: Chapters 1, 6, 7, 8, 13, 14, 15, 18.
10. Overprovision capacity vs. overprovision connectivity: Chapters 14, 15, 16.
11. Feedback control: Chapters 1, 7, 13, 14.
12. Utility maximization: Chapters 1, 2, 11, 12, 14, 20.
13. Protocols: Chapters 14, 15, 17, 19.
14. Signaling: Chapters 6, 19.
15. Randomization: Chapters 3, 15, 18.
16. Graph consistency models: Chapters 3, 13.

17. Strategic equilibrium models: Chapters 1, 2, 15.
18. Generative model (and reverse engineering): Chapters 9, 10, 14.
19. Latent-factor models: Chapter 4.
20. Axiomatization models: Chapters 6, 20.

In the first offering of this course at Princeton, the undergrads voted (by Borda count) “resource sharing,” “opinion aggregation,” and “positive network effect” as the top three concepts they found most useful. They also voted the key equations in PageRank, distributed power control, and Bellman–Ford as the top three equations.

Almost every one of these 20 ideas cuts across social/economic networks and technological networks. Some examples are given below.

- The emergence of global coordination through local actions based on local views is a recurring theme, from influence models in social networks to routing and congestion control in the Internet, and from consumer reaction to pricing signals to power control in wireless networks.
- Resource sharing models, in the form of additive sharing $x + y \leq 1$, or multiplicative sharing $x/y \geq 1$, or binary sharing $x, y \in \{0, 1\}, x + y \leq 1$, are introduced for network pricing as well as the classic problems of congestion control, power control, and contention control.
- The (positive) network effect is often highlighted in social and economic networks. It also finds a concrete realization in how content is shared over the Internet through peer-to-peer protocols and how data centers are scaled up.
- “The wisdom of (independent and unbiased) crowds” is another common theme. There are two types of “wisdom” here. (1) Diversity gain in reducing the chance of some bad event (typically represented mathematically by $1 - (1 - p)^N$, where N is the size of the crowd and p the probability of some bad event). (2) Efficiency gain in smoothing out some average metric (typically represented mathematically as a factor- N in the metric). Both types are observed in social networks and in the latest generation of 4G and WiFi wireless networks.
- Consensus formation is used in computing webpage importance scores in PageRank as well as in discovering the right time to transmit in WiFi.
- Spatial hierarchy is used both in how search is done in a small world and in how the Internet is structured.
- The design methodology of feedback control is used in influence models in social networks and congestion control in the Internet.
- Utility maximization is used in auctioning advertising spots and setting Internet access pricing.
- The power method is used both in Google’s PageRank and in Qualcomm’s distributed power control.
- Randomization is used in PageRank and 802.11 CSMA.
- Strategic equilibrium models are used in auctioning and BitTorrent.

- Reverse engineering is used in studying scale-free networks and TCP.
- Axiomatization is used in voting procedure and fairness evaluation.

This list goes on. Yet equally important are the subtle differences between technological and socio-economic networks. Exhibit A for this alert is the (non-existence of) the Achilles' heel of the Internet and the debate between two generative models (preferential attachment vs. constrained optimization) of scale-free networks.

Two Bigger Pictures

There are two broader themes in the backdrop of this book:

- *Instill domain-specific functionalities to a generic network science.* A “network science” around these 20 questions must be based on domain-specific models and on the pursuit of falsification. For example, while a random graph is elegant, it's often neither a relevant approach to design nor the only generative model to explain what we see in this book. And as much as metrics of a static graph are important, engineering protocols governing the *functionalities* of feedback, coordination, and robustness are just as crucial as the *topological* properties of the graph like the degree distribution.
- *Revisit the Electrical and Computer Engineering (ECE) undergraduate curriculum.* In the standard curriculum in ECE since around the 1960s, a “signals and systems” course is one of the first foundational courses. As networks of various kinds play an increasingly important role both in engineering design and in the society, it's time to capture fundamental concepts in networking in a second systems course. Just as linear time-invariant systems, sampling, integral transforms, and filter design have laid the foundation of ECE curriculum since the 1960s, we think the following concepts have now become fundamental to teach to future ECE students (whether they are taught in the JIT way or not): patterns of connections among nodes, modularization and hierarchy in networked systems, consistency and consensus in graphs, distributed coordination by pricing feedback, strategic equilibrium in competition and cooperation, pros and cons of scaling up, etc.

So this book is an experiment in both *what* to teach and *how* to teach in an ECE undergraduate course in systems: what constitutes core knowledge that needs to be taught and how to teach it in a context that enhances learning efficiency. As much as we appreciate FIR and IIR filter design, Laplace and Z transforms, etc., maybe it's about time to explore the possibility of reducing the coverage of these topics by just a tiny bit to make room for mathematical notions just as fundamental to engineering today. And we believe the best way to drive home these ideas is to tie in with applications that teenagers, and many of the older folks, use every day.

Class as a Social and Economic Network

The class “Networks: Friends, Money, and Bytes,” created in parallel to this book in Fall 2011 and cross-listed in EE and CS at Princeton University, was a social and economic network itself. We tweeted, we blogged, and we created wikis. On the first day of the class, we drew a class social graph, where each node is a student, and a link represents a “know by first name before coming to the first lecture” relationship. After the last lecture, we drew the graph again.

We also created our own currency called “nuggets.” The TAs and I “printed” our money as we saw fit. There were several standard ways to earn nuggets, including catching typos in lecture notes and writing popular blogs. There were ten class activities beyond homework problems that were rewarded by nuggets, including one activity in which the students were allowed to buy and sell their homework solutions using auctions. The matching of students and class project topics was also run through bidding with nuggets. Eventually the nugget balances translate into an upward adjustment of grades. To see some of the fun of ELE/COS 381 at Princeton University, visit www.network20q.com.

Starting in Fall 2012, this course is offered on Stanford’s coursera and its own open education course website, and on YouTube and iTunes U too. The Princeton offering adopts the approach of flipped classroom advocated by the Khan Academy. With many parallel, on-going efforts from different universities and companies (CodeAcademy, coursera, EdX, udacity, etc.), it will take a few years before the landscape of open online education becomes stable. Higher education will be enhanced by this movement that has been gathering momentum since MIT’s open courseware initiative in 2002. Yet many issues remain to settle at the time of writing this book: the modes and efficiency of students’ learning, the boundary and reach of higher education, the prioritization and value propositions of a university’s missions, the roles of faculty and the nature of classroom teaching, the differentiation between self-education and branded-certification, the authenticity and ownership of student-activity records, the tuition revenue to universities and business models of open access platforms, the drawbacks of monetization on for-profit platforms... What is already clear, however, is that this mode of education cannot be feasible without the widespread use of mobile data devices, the video-watching habit of the YouTube generation, or the crowd-sourcing of social-networked online study group. These are exactly some of the key topics studied in this course. From voting of popular questions to distributing video over 4G networks, this is a course *about* these networks and taught *through* these networks.