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978-1-107-01614-9 - Malliavin Calculus for Lévy Processes and Infinite-Dimensional Brownian Motion: An Introduction

Horst Osswald

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