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978-1-107-00056-8 - Quasilinear Control: Performance Analysis and Design of Feedback Systems with Nonlinear Sensors and Actuators

ShiNung Ching, Yongsoon Eun, Cevat Gokcek, Pierre T. Kabamba and Semyon M. Meerkov

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