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978-0-521-87483-0 - Intermediate Dynamics for Engineers: A Unified Treatment of Newton-Euler and Lagrangian Mechanics

Oliver M. O'Reilly

Table of Contents

[More information](#)

Contents

<i>Preface</i>	<i>page xi</i>
PART ONE DYNAMICS OF A SINGLE PARTICLE	1
1 Kinematics of a Particle	3
1.1 Introduction	3
1.2 Reference Frames	3
1.3 Kinematics of a Particle	5
1.4 Frequently Used Coordinate Systems	6
1.5 Curvilinear Coordinates	9
1.6 Representations of Particle Kinematics	14
1.7 Constraints	15
1.8 Classification of Constraints	20
1.9 Closing Comments	27
Exercises	27
2 Kinetics of a Particle	33
2.1 Introduction	33
2.2 The Balance Law for a Single Particle	33
2.3 Work and Power	35
2.4 Conservative Forces	36
2.5 Examples of Conservative Forces	37
2.6 Constraint Forces	39
2.7 Conservations	45
2.8 Dynamics of a Particle in a Gravitational Field	47
2.9 Dynamics of a Particle on a Spinning Cone	55
2.10 A Shocking Constraint	59
2.11 A Simple Model for a Roller Coaster	60
2.12 Closing Comments	64
Exercises	66

3 Lagrange's Equations of Motion for a Single Particle	70
3.1 Introduction	70
3.2 Lagrange's Equations of Motion	71
3.3 Equations of Motion for an Unconstrained Particle	73
3.4 Lagrange's Equations in the Presence of Constraints	74
3.5 A Particle Moving on a Sphere	78
3.6 Some Elements of Geometry and Particle Kinematics	80
3.7 The Geometry of Lagrange's Equations of Motion	83
3.8 A Particle Moving on a Helix	87
3.9 Summary	91
Exercises	92
 PART TWO DYNAMICS OF A SYSTEM OF PARTICLES	 101
4 The Equations of Motion for a System of Particles	103
4.1 Introduction	103
4.2 A System of N Particles	104
4.3 Coordinates	105
4.4 Constraints and Constraint Forces	107
4.5 Conservative Forces and Potential Energies	110
4.6 Lagrange's Equations of Motion	111
4.7 Construction and Use of a Single Representative Particle	113
4.8 The Lagrangian	118
4.9 A Constrained System of Particles	119
4.10 A Canonical Form of Lagrange's Equations	122
4.11 Alternative Principles of Mechanics	128
4.12 Closing Remarks	131
Exercises	131
5 Dynamics of Systems of Particles	134
5.1 Introduction	134
5.2 Harmonic Oscillators	134
5.3 A Dumbbell Satellite	140
5.4 A Pendulum and a Cart	143
5.5 Two Particles Tethered by an Inextensible String	147
5.6 Closing Comments	151
Exercises	153
 PART THREE DYNAMICS OF A SINGLE RIGID BODY	 161
6 Rotation Tensors	163
6.1 Introduction	163
6.2 The Simplest Rotation	164
6.3 Proper-Orthogonal Tensors	166
6.4 Derivatives of a Proper-Orthogonal Tensor	168

Cambridge University Press

978-0-521-87483-0 - Intermediate Dynamics for Engineers: A Unified Treatment of Newton-Euler and Lagrangian Mechanics

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Table of Contents

[More information](#)

Contents

ix

6.5	Euler's Representation of a Rotation Tensor	171
6.6	Euler's Theorem: Rotation Tensors and Proper-Orthogonal Tensors	176
6.7	Relative Angular Velocity Vectors	178
6.8	Euler Angles	181
6.9	Further Representations of a Rotation Tensor	191
6.10	Derivatives of Scalar Functions of Rotation Tensors	195
	Exercises	198
7	Kinematics of Rigid Bodies	206
7.1	Introduction	206
7.2	The Motion of a Rigid Body	206
7.3	The Angular Velocity and Angular Acceleration Vectors	211
7.4	A Corotational Basis	212
7.5	Three Distinct Axes of Rotation	213
7.6	The Center of Mass and Linear Momentum	215
7.7	Angular Momenta	218
7.8	Euler Tensors and Inertia Tensors	219
7.9	Angular Momentum and an Inertia Tensor	223
7.10	Kinetic Energy	224
7.11	Concluding Remarks	226
	Exercises	226
8	Constraints on and Potentials for Rigid Bodies	237
8.1	Introduction	237
8.2	Constraints	237
8.3	A Canonical Function	241
8.4	Integrability Criteria	243
8.5	Forces and Moments Acting on a Rigid Body	247
8.6	Constraint Forces and Constraint Moments	248
8.7	Potential Energies and Conservative Forces and Moments	256
8.8	Concluding Comments	262
	Exercises	263
9	Kinetics of a Rigid Body	272
9.1	Introduction	272
9.2	Balance Laws for a Rigid Body	272
9.3	Work and Energy Conservation	274
9.4	Additional Forms of the Balance of Angular Momentum	276
9.5	Moment-Free Motion of a Rigid Body	279
9.6	The Baseball and the Football	285
9.7	Motion of a Rigid Body with a Fixed Point	289
9.8	Motions of Rolling Spheres and Sliding Spheres	294
9.9	Closing Comments	297
	Exercises	299

Cambridge University Press

978-0-521-87483-0 - Intermediate Dynamics for Engineers: A Unified Treatment of Newton-Euler and Lagrangian Mechanics

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Table of Contents

[More information](#)

x

Contents

10 Lagrange's Equations of Motion for a Single Rigid Body	307
10.1 Introduction	307
10.2 Configuration Manifold of an Unconstrained Rigid Body	308
10.3 Lagrange's Equations of Motion: A First Form	311
10.4 A Satellite Problem	315
10.5 Lagrange's Equations of Motion: A Second Form	318
10.6 Lagrange's Equations of Motion: Approach II	324
10.7 Rolling Disks and Sliding Disks	325
10.8 Lagrange and Poisson Tops	331
10.9 Closing Comments	336
Exercises	336
 PART FOUR SYSTEMS OF RIGID BODIES	 345
11 Introduction to Multibody Systems	347
11.1 Introduction	347
11.2 Balance Laws and Lagrange's Equations of Motion	347
11.3 Two Pin-Jointed Rigid Bodies	349
11.4 A Single-Axis Rate Gyroscope	351
11.5 Closing Comments	355
Exercises	355
 APPENDIX: BACKGROUND ON TENSORS	 362
A.1 Introduction	362
A.2 Preliminaries: Bases, Alternators, and Kronecker Deltas	362
A.3 The Tensor Product of Two Vectors	363
A.4 Second-Order Tensors	364
A.5 A Representation Theorem for Second-Order Tensors	364
A.6 Functions of Second-Order Tensors	367
A.7 Third-Order Tensors	370
A.8 Special Types of Second-Order Tensors	372
A.9 Derivatives of Tensors	373
Exercises	374
 <i>Bibliography</i>	 377
<i>Index</i>	389