

Nonparametric System Identification

Presenting a thorough overview of the theoretical foundations of nonparametric systems identification for nonlinear block-oriented systems, Włodzimierz Greblicki and Mirosław Pawlak show that nonparametric regression can be successfully applied to system identification, and they highlight what you can achieve in doing so.

Starting with the basic ideas behind nonparametric methods, various algorithms for nonlinear block-oriented systems of cascade and parallel forms are discussed in detail. Emphasis is placed on the most popular systems, Hammerstein and Wiener, which have applications in engineering, biology, and financial modeling.

Algorithms using trigonometric, Legendre, Laguerre, and Hermite series are investigated, and the kernel algorithm, its semirecursive versions, and fully recursive modifications are covered. The theories of modern nonparametric regression, approximation, and orthogonal expansions are also provided, as are new approaches to system identification. The authors show how to identify nonlinear subsystems so that their characteristics can be obtained even when little information exists, which is of particular significance for practical application. Detailed information about all the tools used is provided in the appendices.

This book is aimed at researchers and practitioners in systems theory, signal processing, and communications. It will also appeal to researchers in fields such as mechanics, economics, and biology, where experimental data are used to obtain models of systems.

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Both authors have published extensively over the years in the area of nonparametric theory and applications.

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Włodzimierz Greblicki , Mirosław Pawlak
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Nonparametric System Identification

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To my wife, Helena, and my children, Jerzy, Maria, and Magdalena – WG
To my parents and family and those whom I love – MP

Preface

The aim of this book is to show that the nonparametric regression can be applied successfully to nonlinear system identification. It gathers what has been done in the area so far and presents main ideas, results, and some new recent developments.

The study of nonparametric regression estimation began with works published by Cencov, Watson, and Nadaraya in the 1960s. The history of nonparametric regression in system identification began about ten years later. Such methods have been applied to the identification of composite systems consisting of nonlinear memoryless systems and linear dynamic ones. Therefore, the approach is strictly connected with so-called block-oriented methods developed since Narendra and Gallman's work published in 1966. Hammerstein and Wiener structures are most popular and have received the greatest attention in numerous applications. Fundamental for nonparametric methods is the observation that the unknown characteristic of the nonlinear subsystem or its inverse can be represented as regression functions.

In terms of the a priori information, standard identification methods and algorithms work when it is parametric, that is, when our knowledge about the system is rather large; for example, when we know that the nonlinear subsystem has a polynomial characteristic. In this book, the information is much smaller, nonparametric. The mentioned characteristic can be, for example, any integrable or bounded or, even, any Borel function.

It can thus be said that this book associates block-oriented system identification with nonparametric regression estimation and shows how to identify nonlinear subsystems, that is, to recover their characteristics when the a priori information is small. Because of this, the approach should be of interest not only to researchers but also to people interested in applications.

Chapters 2–7 are devoted to discrete-time Hammerstein systems. Chapter 2 presents basic discussion of the Hammerstein system and its relationship with the concept of the nonparametric regression. The nonparametric kernel algorithm is presented in Chapter 3, its semirecursive versions are examined in Chapter 4, and Chapter 5 deals with fully recursive modifications derived from the idea of stochastic approximation. Next, Chapter 6 is concerned with the nonparametric orthogonal series method. Algorithms using trigonometric, Legendre, Laguerre, and Hermite series are investigated. Some space is devoted to estimation methods based on wavelets. Nonparametric algorithms based on ordered observations are presented and examined in Chapter 7. Chapter 8 discusses the nonparametric algorithms when applied to continuous-time Hammerstein systems.

The Wiener system is identified in Chapters 9–11. Chapter 9 presents the motivation for nonparametric algorithms that are studied in the next two chapters devoted to the discrete and continuous-time Wiener systems, respectively. Chapter 12 is concerned with the generalization of our theory to other block-oriented nonlinear systems. This includes, among others, parallel models, cascade-parallel models, sandwich models, and generalized Hammerstein systems possessing local memory. In Chapter 13, the multivariate versions of block-oriented systems are examined. The common problem of multivariate systems, that is, the curse of dimensionality, is cured by using low-dimensional approximations. With respect to this issue, models of the additive form are introduced and examined. In Chapter 14, we develop identification algorithms for a semiparametric class of block-oriented systems. Such systems are characterized by a mixture of finite dimensional parameters and nonparametric functions being typically a set of univariate functions.

The reader is encouraged to look into the appendices, in which fundamental information about tools used in the book is presented in detail. Appendix A is strictly related to kernel algorithms, and Appendix B is tied with the orthogonal series nonparametric curve estimates. Appendix C recalls some facts from probability theory and presents results from the theory of order statistics used extensively in Chapter 7.

Over the years, our work has benefited greatly from the advice and support of a number of friends and colleagues with interest in ideas of nonparametric estimation, pattern recognition, and nonlinear system modeling. There are too many names to list here, but special mention is due to Adam Krzyżak, as well as Danuta Rutkowska, Leszek Rutkowski, Alexander Georgiev, Simon Liao, Pradeepa Yahampath, and Yongqing Xin – our past Ph.D. students, now professors at universities in Canada, the United States, and Poland. Cooperation with them has been a great pleasure and given us a lot of satisfaction. We are deeply indebted to Zygmunt Hasiwicz, Ewaryst Rafajłowicz, Uli Stadtmüller, Ewa Rafajłowicz, Hajo Holzmann, and Andrzej Kozek, who have contributed greatly to our research in the area of nonlinear system identification, pattern recognition, and nonparametric inference.

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