

Econometric Exercises, Volume 7

Bayesian Econometric Methods

This book is a volume in the Econometric Exercises series. It teaches principles of Bayesian econometrics by posing a series of theoretical and applied questions, and providing detailed solutions to those questions. This text is primarily suitable for graduate study in econometrics, though it can be used for advanced undergraduate courses, and should generate interest from students in related fields, including finance, marketing, agricultural economics, business economics, and other disciplines that employ statistical methods. The book provides a detailed treatment of a wide array of models commonly employed by economists and statisticians, including linear regression-based models, hierarchical models, latent variable models, mixture models, and time series models. Basics of random variable generation and simulation via Markov Chain Monte Carlo (MCMC) methods are also provided. Finally, posterior simulators for each type of model are rigorously derived, and Matlab computer programs for fitting these models (using both actual and generated data sets) are provided on the Web site accompanying the text.

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Econometric Exercises

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Bayesian Econometric Methods

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To Lise
To the Reverend but not the Queen
To Melissa, Madeline, and Drew

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Preface to the series

The past two decades have seen econometrics grow into a vast discipline. Many different branches of the subject now happily coexist with one another. These branches interweave econometric theory and empirical applications and bring econometric method to bear on a myriad of economic issues. Against this background, a guided treatment of the modern subject of econometrics in volumes of worked econometric exercises seemed a natural and rather challenging idea.

The present series, *Econometric Exercises*, was conceived in 1995 with this challenge in mind. Now, almost a decade later it has become an exciting reality with the publication of the first installment of a series of volumes of worked econometric exercises. How can these volumes work as a tool of learning that adds value to the many existing textbooks of econometrics? What readers do we have in mind as benefiting from this series? What format best suits the objective of helping these readers learn, practice, and teach econometrics? These questions we now address, starting with our overall goals for the series.

Econometric Exercises is published as an organized set of volumes. Each volume in the series provides a coherent sequence of exercises in a specific field or subfield of econometrics. Solved exercises are assembled together in a structured and logical pedagogical framework that seeks to develop the subject matter of the field from its foundations through to its empirical applications and advanced reaches. As the Schaum series has done so successfully for mathematics, the overall goal of *Econometric Exercises* is to develop the subject matter of econometrics through solved exercises, providing a coverage of the subject that begins at an introductory level and moves through to more advanced undergraduate- and graduate-level material.

Problem solving and worked exercises play a major role in every scientific subject. They are particularly important in a subject like econometrics in which there is a rapidly growing literature of statistical and mathematical technique and an ever-expanding core to the discipline. As students, instructors, and researchers, we all benefit by seeing carefully

worked-out solutions to problems that develop the subject and illustrate its methods and workings. Regular exercises and problem sets consolidate learning and reveal applications of textbook material. Clearly laid out solutions, paradigm answers, and alternate routes to solution all develop problem-solving skills. Exercises train students in clear analytical thinking and help them in preparing for tests and exams. Teachers, as well as students, find solved exercises useful in their classroom preparation and in designing problem sets, tests, and examinations. Worked problems and illustrative empirical applications appeal to researchers and professional economists wanting to learn about specific econometric techniques. Our intention for the *Econometric Exercises* series is to appeal to this wide range of potential users.

Each volume of the series follows the same general template. Chapters begin with a short outline that emphasizes the main ideas and overviews the most relevant theorems and results. The introductions are followed by a sequential development of the material by solved examples and applications, and by computer exercises when appropriate. All problems are solved and they are graduated in difficulty with solution techniques evolving in a logical, sequential fashion. Problems are asterisked when they require more creative solutions or reach higher levels of technical difficulty. Each volume is self-contained. There is some commonality in material across volumes to reinforce learning and to make each volume accessible to students and others who are working largely, or even completely, on their own.

Content is structured so that solutions follow immediately after the exercise is posed. This makes the text more readable and avoids repetition of the statement of the exercise when it is being solved. More importantly, posing the right question at the right moment in the development of a subject helps to anticipate and address future learning issues that students face. Furthermore, the methods developed in a solution and the precision and insights of the answers are often more important than the questions being posed. In effect, the inner workings of a good solution frequently provide benefit beyond what is relevant to the specific exercise.

Exercise titles are listed at the start of each volume, following the table of contents, so that readers may see the overall structure of the book and its more detailed contents. This organization reveals the exercise progression, how the exercises relate to one another, and where the material is heading. It should also tantalize readers with the exciting prospect of advanced material and intriguing applications.

The series is intended for a readership that includes undergraduate students of econometrics with an introductory knowledge of statistics, first- and second-year graduate students of econometrics, as well as students and instructors from neighboring disciplines (such as statistics, psychology, or political science) with interests in econometric methods. The volumes generally increase in difficulty as the topics become more specialized.

The early volumes in the series (particularly those covering matrix algebra, statistics, econometric models, and empirical applications) provide a foundation to the study of econometrics. These volumes will be especially useful to students who are following the first-year econometrics course sequence in North American graduate schools and need to prepare for

graduate comprehensive examinations in econometrics and to write an applied econometrics paper. The early volumes will equally be of value to advanced undergraduates studying econometrics in Europe, to advanced undergraduates and honors students in the Australasian system, and to masters and doctoral students in general. Subsequent volumes will be of interest to professional economists, applied workers, and econometricians who are working with techniques in those areas, as well as students who are taking an advanced course sequence in econometrics and statisticians with interests in those topics.

The *Econometric Exercises* series is intended to offer an independent learning-by-doing program in econometrics and it provides a useful reference source for anyone wanting to learn more about econometric methods and applications. The individual volumes can be used in classroom teaching and examining in a variety of ways. For instance, instructors can work through some of the problems in class to demonstrate methods as they are introduced; they can illustrate theoretical material with some of the solved examples; and they can show real data applications of the methods by drawing on some of the empirical examples. For examining purposes, instructors may draw freely from the solved exercises in test preparation. The systematic development of the subject in individual volumes will make the material easily accessible both for students in revision and for instructors in test preparation.

In using the volumes, students and instructors may work through the material sequentially as part of a complete learning program, or they may dip directly into material in which they are experiencing difficulty to learn from solved exercises and illustrations. To promote intensive study, an instructor might announce to a class in advance of a test that some questions in the test will be selected from a certain chapter of one of the volumes. This approach encourages students to work through most of the exercises in a particular chapter by way of test preparation, thereby reinforcing classroom instruction.

Further details and updated information about individual volumes can be obtained from the *Econometric Exercises* Web site:

<http://us.cambridge.org/economics/ee/econometricexercises.htm>

The Web site also contains the basic notation for the series, which can be downloaded along with the \LaTeX style files.

As series editors, we welcome comments, criticisms, suggestions, and, of course, corrections from all our readers on each of the volumes in the series as well as on the series itself. We bid you as much happy reading and problem solving as we have had in writing and preparing this series.

York, Tilburg, New Haven
June 2005

Karim M. Abadir
Jan R. Magnus
Peter C. B. Phillips

Preface

Bayesian econometrics has enjoyed an increasing popularity in many fields. This popularity has been evidenced through the recent publication of several textbooks at the advanced undergraduate and graduate levels, including those by Poirier (1995), Bauwens, Lubrano, and Richard (1999), Koop (2003), Lancaster (2004), and Geweke (2005). The purpose of the present volume is to provide a wide range of exercises and solutions suitable for students interested in Bayesian econometrics at the level of these textbooks.

The Bayesian researcher should know the basic ideas underlying Bayesian methodology (i.e., Bayesian theory) and the computational tools used in modern Bayesian econometrics (i.e., Bayesian computation). The Bayesian should also be able to put the theory and computational tools together in the context of substantive empirical problems. We have written this book with these three activities – theory, computation, and empirical modeling – in mind. We have tried to construct a wide range of exercises on all of these aspects. Loosely speaking, Chapters 1 through 9 focus on Bayesian theory, whereas Chapter 11 focuses primarily on recent developments in Bayesian computation. The remaining chapters focus on particular models (usually regression based). Inevitably, these chapters combine theory and computation in the context of particular models. Although we have tried to be reasonably complete in terms of covering the basic ideas of Bayesian theory and the computational tools most commonly used by the Bayesian, there is no way we can cover all the classes of models used in econometrics. Accordingly, we have selected a few popular classes of models (e.g., regression models with extensions and panel data models) to illustrate how the Bayesian paradigm works in practice. Particularly in Chapters 12 through 18 we have included substantive empirical exercises – some of them based closely on journal articles. We hope that the student who works through these chapters will have a good feeling for how serious Bayesian empirical work is done and will be well placed to write a Ph.D. dissertation or a journal article using Bayesian methods.

For the student with limited time, we highlight that a division in this book occurs between the largely theoretical material of Chapters 1 through 9 and the largely regression-based material in Chapters 10 through 18. A student taking a course on Bayesian statistical theory could focus on Chapters 1 through 9, whereas a student taking a Bayesian econometrics course (or interested solely in empirical work) could focus more on Chapters 10 through 18 (skimming through the more methodologically oriented material in the early chapters).

Although there have been some attempts to create specifically Bayesian software (e.g., BUGS, which is available at <http://www.mrc-bsu.cam.ac.uk/bugs>, or BACC, which is available at <http://www2.cirano.qc.ca/~bacc>), in our estimation, most Bayesians still prefer to create their own programs using software such as Matlab, OX, or GAUSS. We have used Matlab to create answers to the empirical problems in this book. Our Matlab code is provided on the Web site associated with this book:

http://www.econ.iastate.edu/faculty/tobias/Bayesian_exercises.html

A few notational conventions are applied throughout the book, and it is worthwhile to review some of these prior to diving into the exercises. In regression-based problems, which constitute a majority of the exercises in the later chapters, lowercase letters such as y and x_i are reserved to denote scalar or vector quantities whereas capitals such as X or X_j are used to denote matrices. In cases in which the distinction between vectors and scalars is critical, this will be made clear within the exercise. In the regression-based problems, y is assumed to denote the $n \times 1$ vector of stacked responses for the dependent variable, y_i the i th element of that vector, x_i a k vector of covariate data, and X the $n \times k$ matrix obtained from stacking the x_i over i . Latent variables, which are often utilized in the computational chapters of the book, are typically designated with a “*” superscript, such as y_i^* . In Chapters 1 through 9, many exercises are presented that are not directly related to linear regression models or models that can be viewed as linear on suitably defined latent data. In these exercises, the distinction between random variables and realizations of those variables is sometimes important. In such cases, we strive to use capital letters to denote random variables, which are unknown *ex ante*, and lowercase letters to denote their realizations, which are known *ex post*. So, in the context of discussing a posterior distribution (which conditions on the data), we will use \bar{y} , but if we are interested in discussing the sampling properties of the sample mean, \bar{Y} would be the appropriate notation. Finally, “ \times ” is used to denote multiplication in multiline derivations, and specific parameterizations of various densities are provided in the Appendix associated with this book.

On the issue of parameterization, the reader who is somewhat familiar with the Bayesian literature may realize that researchers often employ different parameterizations for the same model, with no particular choice being “correct” or “ideal.” A leading example is the linear regression model, in which the researcher can choose to parameterize this model in terms of the error variance or the error precision (the reciprocal of the variance). In this book, we try and remain consistent in terms of parameterization within individual chapters, though some departures from this trend do exist, particularly in Chapters 11 and 16. These differences arise from our own individual tastes and styles toward approaching these models, and they

are superficial rather than substantive. In our view it is quite valuable to expose the student to the use of different parameterizations, since this is the reality that he or she will face when exploring the Bayesian literature in more detail. In all cases, the parameterization employed is clearly delineated within each exercise.

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