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978-0-521-83490-2 - Multiple Scattering of Light by Particles: Radiative Transfer and Coherent Backscattering

Michael I. Mishchenko, Larry D. Travis and Andrew A. Lacis

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