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978-0-521-80717-3 - Industrial Mathematics: Case Studies in the Diffusion of Heat and Matter

Glenn R. Fulford and Philip Broadbridge

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