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978-0-521-76914-3 - Structures in the Universe by Exact Methods: Formation, Evolution, Interactions

Krzysztof Bolejko, Andrzej Krasinski, Charles Hellaby and Marie-Noelle Celerier

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