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978-0-521-76867-2 - Dynamics of the Standard Model: Second Edition

John F. Donoghue, Eugene Golowich and Barry R. Holstein

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