

Cambridge University Press

978-0-521-76655-5 - Discrete Choice Methods with Simulation, Second Edition

Kenneth E. Train

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Discrete Choice Methods with Simulation

Second Edition

This book describes the new generation of discrete choice methods, focusing on the many advances that are made possible by simulation. Researchers use these statistical methods to examine the choices that consumers, households, firms, and other agents make. Each of the major models is covered: logit, generalized extreme value (including nested and cross-nested logits), probit, and mixed logit, plus a variety of specifications that build on these basics. Simulation-assisted estimation procedures are investigated and compared, including maximum simulated likelihood, method of simulated moments, and method of simulated scores. Procedures for drawing from densities are described, including variance reduction techniques such as antithetics and Halton draws. Recent advances in Bayesian procedures are explored, including the use of the Metropolis–Hastings algorithm and its variant Gibbs sampling. This second edition adds chapters on endogeneity and expectation-maximization algorithms. No other book incorporates all these topics, which have arisen in the past 25 years. The procedures are applicable in many fields, including energy, transportation, environmental studies, health, labor, and marketing.

Professor Kenneth E. Train teaches econometrics, regulation, and industrial organization at the University of California, Berkeley. He also serves as Vice President of National Economic Research Associates (NERA), Inc., in San Francisco, California. The author of *Optimal Regulation: The Economic Theory of Natural Monopoly* (1991) and *Qualitative Choice Analysis* (1986), Dr. Train has written more than 60 articles on economic theory and regulation. He chaired the Center for Regulatory Policy at the University of California, Berkeley, from 1993 to 2000 and has testified as an expert witness in regulatory proceedings and court cases. He has received numerous awards for his teaching and research.

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Additional Praise for the First Edition of *Discrete Choice Methods with Simulation*

“Ken Train’s book provides outstanding coverage of the most advanced elements of the estimation and usage of discrete choice models that require simulation to take account of randomness in the population under study. His writing is clear and understandable, providing both the new and experienced reader with excellent insights into and understanding of all aspects of these new and increasingly important methods.”

– Frank S. Koppelman, *Northwestern University*

“This is a masterful book, authored by one of the leading contributors to discrete choice methods and analysis. No other book covers this ground with such up-to-date detail in respect of theory and implementation. The chapters on simulation and recent developments such as mixed logit are most lucid. As a text or reference work this volume should have currency for a long time. It will appeal to the practitioner as much as to the specialist researcher who has been in this field for many years.”

– David Hensher, *The University of Sydney*

“Simulation-based estimation is a major advance in econometrics and discrete choice modeling. The technique has revolutionized both classical and Bayesian analysis. Ken Train’s many papers have made a large contribution to this literature. *Discrete Choice Methods with Simulation* collects these results in a comprehensive, up-to-date source, with chapters on behavioral foundations, theoretical and practical aspects of estimation, and a variety of applications. This book is a thoroughly enjoyable blend of theory, analysis, and case studies; it is a complete reference for developers and practitioners.”

– William Greene, *New York University*

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*To
Daniel McFadden
and
in memory of
Kenneth Train, Sr.*

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