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978-0-521-76456-8 - Strategic Financial Planning over the Lifecycle: A Conceptual Approach to Personal Risk Management

Narat Charupat, Huaxiong Huang and Moshe A. Milevsky

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