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978-0-521-20016-5 - The Large Scale Structure of Space-Time

S. W. Hawking, F.R.S. and G. F. R. Ellis

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