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978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

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Evaluating Learning Algorithms

The field of machine learning has matured to the point where many sophisticated learning approaches can be applied to practical applications. Thus it is of critical importance that researchers have the proper tools to evaluate learning approaches and understand the underlying issues.

This book examines various aspects of the evaluation process with an emphasis on classification algorithms. The authors describe several techniques for classifier performance assessment, error estimation and resampling, and obtaining statistical significance, as well as selecting appropriate domains for evaluation. They also present a unified evaluation framework and highlight how different components of evaluation are both significantly interrelated and interdependent. The techniques presented in the book are illustrated using R and WEKA, facilitating better practical insight as well as implementation.

Aimed at researchers in the theory and applications of machine learning, this book offers a solid basis for conducting performance evaluations of algorithms in practical settings.

Nathalie Japkowicz is a Professor of Computer Science at the School of Information Technology and Engineering of the University of Ottawa. She also taught machine learning and artificial intelligence at Dalhousie University and Ohio State University. Along with machine learning evaluation, her research interests include one-class learning, the class imbalance problem, and learning in the presence of concept drifts.

Mohak Shah is a Postdoctoral Fellow at McGill University. He earned a PhD in Computer Science from the University of Ottawa in 2006 and was a Postdoctoral Fellow at CHUL Genomics Research Center in Quebec prior to joining McGill. His research interests span machine learning and statistical learning theory as well as their application to various domains.

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A Classification Perspective

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Frontmatter

[More information](#)

This book is dedicated to the memory of my father, Michel Japkowicz (1935–2008), who was my greatest supporter all throughout my studies and career, taking a great interest in any project of mine. He was aware of the fact that this book was being written, encouraged me to write it, and would be the proudest father on earth to see it in print today.

Nathalie

This book is dedicated to the loving memory of my father, Upendra Shah (1948–2006), who was my mentor in life. He taught me the importance of not falling for means but looking for meaning in life. He was also my greatest support through all times, good and bad. His memories are a constant source of inspiration and motivation. Here's to you Dad!

Mohak

Contents

Preface	<i>page xi</i>
Acronyms	xv
1 Introduction	1
1.1 The De Facto Culture	3
1.2 Motivations for This Book	6
1.3 The De Facto Approach	7
1.4 Broader Issues with Evaluation Approaches	12
1.5 What Can We Do?	16
1.6 Is Evaluation an End in Itself?	18
1.7 Purpose of the Book	19
1.8 Other Takes on Evaluation	20
1.9 Moving Beyond Classification	20
1.10 Thematic Organization	21
2 Machine Learning and Statistics Overview	23
2.1 Machine Learning Overview	23
2.2 Statistics Overview	42
2.3 Summary	72
2.4 Bibliographic Remarks	73
3 Performance Measures I	74
3.1 Overview of the Problem	75
3.2 An Ontology of Performance Measures	81
3.3 Illustrative Example	82
3.4 Performance Metrics with a Multiclass Focus	85
3.5 Performance Metrics with a Single-Class Focus	94
3.6 Illustration of the Confusion-Matrix-Only-Based Metrics Using WEKA	107

Cambridge University Press

978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

viii

Contents

3.7	Summary	108
3.8	Bibliographic Remarks	109
4	Performance Measures II	111
4.1	Graphical Performance Measures	112
4.2	Receiver Operating Characteristic (ROC) Analysis	112
4.3	Other Visual Analysis Methods	131
4.4	Continuous and Probabilistic Classifiers	137
4.5	Specialized Metrics	143
4.6	Illustration of the Ranking and Probabilistic Approaches Using R, ROCR, and WEKA	146
4.7	Summary	159
4.8	Bibliographic Remarks	159
5	Error Estimation	161
5.1	Introduction	163
5.2	Holdout Approach	164
5.3	What Implicitly Guides Resampling?	167
5.4	Simple Resampling	171
5.5	A Note on Model Selection	177
5.6	Multiple Resampling	178
5.7	Discussion	185
5.8	Illustrations Using R	187
5.9	Summary	202
5.10	Bibliographic Remarks	202
	Appendix: Proof of Equation (5.5)	204
6	Statistical Significance Testing	206
6.1	The Purpose of Statistical Significance Testing	207
6.2	The Limitations of Statistical Significance Testing	210
6.3	An Overview of Relevant Statistical Tests	213
6.4	A Note on Terminology	215
6.5	Comparing <i>Two Classifiers</i> on a <i>Single Domain</i>	217
6.6	Comparing <i>Two Classifiers</i> on <i>Multiple Domains</i>	231
6.7	Comparing <i>Multiple Classifiers</i> on <i>Multiple Domains</i>	239
6.8	Statistical Tests for Two Classifiers on a Single Domain Based on Resampling Techniques	258
6.9	Illustration of the Statistical Tests Application Using R	263
6.10	Summary	289
6.11	Bibliographic Remarks	290
7	Datasets and Experimental Framework	292
7.1	Repository-Based Approach	294
7.2	Making Sense of Our Repositories: Metalearning	300

Cambridge University Press

978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

Contents

ix

7.3	Artificial Data Approach	301
7.4	Community Participation: Web-Based Solutions	304
7.5	Summary	306
7.6	Bibliographic Remarks	306
8	Recent Developments	308
8.1	Performance Metrics	309
8.2	Frameworks for Performance Metrics	312
8.3	Combining Metrics	317
8.4	Insights from Statistical Learning Theory	323
8.5	Other Developments	329
8.6	Summary	330
	Appendix: Proof of Theorems 8.1 and 8.2	330
9	Conclusion	335
9.1	An Evaluation Framework Template	336
9.2	Concluding Remarks	349
9.3	Bibliographic Remarks	350
	Appendix A: Statistical Tables	351
A.1	The Z Table	351
A.2	The t Table	352
A.3	The χ^2 Table	353
A.4	The Table of Critical Values for the Signed Test	355
A.5	The Wilcoxon Table	356
A.6	The F -Ratio Table	357
A.7	The Friedman Table	361
A.8	The Table of Critical Values for the Tukey Test	362
A.9	The Table of Critical Values for the Dunnett Test	363
	Appendix B: Additional Information on the Data	364
	Appendix C: Two Case Studies	368
C.1	Illustrative Case Study 1	368
C.2	Illustrative Case Study 2	375
	Bibliography	393
	Index	403

Cambridge University Press

978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

Preface

This book was started at Monash University (Melbourne, Australia) and Laval University (Quebec City, Canada) with the subsequent writing taking place at the University of Ottawa (Ottawa, Canada) and McGill University (Montreal, Canada). The main idea stemmed from the observation that while machine learning as a field is maturing, the importance of evaluation has not received due appreciation from the developers of learning systems. Although almost all studies make a case for the evaluation of the algorithms they present, we find that many (in fact a majority) demonstrate a limited understanding of the issues involved in proper evaluation, despite the best intention of their authors. We concede that optimal choices cannot always be made due to limiting circumstances, and trade-offs are inevitable. However, the methods adopted in many cases do not reflect attention to the details warranted by a proper evaluation approach (of course there are exceptions and we do not mean to generalize this observation).

Our aim here is not to present the readers with yet another recipe for evaluation that can replace the current default approach. Rather, we try to develop an understanding of and appreciation for the different concerns of importance in the practical application and deployment of learning systems. Once these concerns are well understood, the other pieces of the puzzle fall quickly in place since the researcher is not left shooting in the dark. A proper evaluation procedure consists of many components that should all be considered simultaneously so as to correctly address their interdependence and relatedness. We feel that the best (read most easily understood) manner to bring this holistic view of evaluation to the fore is in the classification setting. Nonetheless, most of the observations that we make with regard to the various evaluation components extend just as well to other learning settings and paradigms since the underlying evaluation principles and objectives are essentially the same.

Altogether, this book should be viewed not only as a tool designed to increase our understanding of the evaluation process in a shared manner, but also as a first

Cambridge University Press

978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

step in the direction of stimulating a community-wide debate on the relevance and importance of the evaluation of learning algorithms.

Incorporating concepts from both machine learning and statistics proved to be a bit more involved than we had first imagined. The main challenge was to integrate the ideas together and present them in a coherent manner. Indeed, sometimes the same terms are used in the two fields to mean different quantities while at other times, the same quantities are referred to by multiple names and notations. We have tried to put some aspects under a unified scheme (of both terminology and notation) but have left others to their more conventional usage, just to make sure that the reader can relate these to other texts. For instance, while we have used α for the confidence parameter in the statistical significance testing, we have also, in some places, used the common notion of p-value to relate to other discussions. Similarly, both P and \Pr frequently appear in probabilistic contexts. We have used both these terms, keeping in mind their common use as well as a better readability of the text. To achieve this, we have used \Pr when referring to events or probabilities for discrete variables. For other cases, e.g., distributions over continuous variables and priors, we use P or other symbols, as indicated in the text. However, with some exceptions, most notations are used locally and explained in their proper context to avoid confusion.

We have tried to illustrate the various methods and tests presented in the book with the use of the freely available R statistical package and WEKA machine learning toolkit. Our code, however, is in no sense optimal. Our main aim here was to illustrate the concepts in the simplest possible manner so that even the least experienced programmers could apply the code easily in order to immediately utilize the tools presented in the book. We hope to post better optimized code on the book Web page in the near future.

While our names figure on the cover, we cannot claim complete credit for the work presented in this book. This work was made possible thanks to the support of many people. The deficiencies or errors, however, are solely due to us. We would now like to take some space to thank them and acknowledge their support, advice, and understanding.

We would like to thank all our colleagues at the various institutions that hosted us while this book was in progress. They helped us form and develop our ideas on evaluation and stimulate our thoughts on various aspects of the problem, either directly or indirectly. These include: Peter Tischer, Ingrid Zuckerman, and Yuval Marom at Monash; Mario Marchand, Jacques Corbeil, and Francois Laviolette at Laval; Stan Matwin and Marcel Turcotte at the University of Ottawa; Chris Drummond and Peter Turney at the University of Ottawa and the National Research Council of Canada; Tal Arbel, D. Louis Collins, Doina Precup, and Douglas L. Arnold at McGill; the graduate students and postdoctoral Fellows William Klement, Guichong Li, Lisa Gaudette, Alex Kouznetsov, and Shiven Sharma at the University at Ottawa; Heidar Pirzadeh and Sara Shanian at Laval; and Dante De Nigris and Simon Francis at McGill. William, Alex,

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Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

Guichong, and Shiven were also instrumental in running certain experiments, checking some of our formulas and code, and helping with the presentation, in various parts of the book. We also benefited greatly from discussions with Rocío Alaiz-Rodríguez during her visit to the University of Ottawa and, later, on-line. Conversations held about evaluation in the context of a collaboration with Health Canada were also quite enlightening and helped shape some of the ideas in this book. In particular, we would like to thank Kurt Ungar, Trevor Stocki, and Ian Hoffman for sharing their thoughts with us, as well as for providing us with data on Radioxenon Monitoring for the Detection of Nuclear Explosions.

Nathalie would like to thank, most particularly, James Malley of the National Institute of Health for helping her recognize the inadequacy of current evaluation practices in machine learning and the repercussions they may have in collaborative settings; and Chris Drummond with whom she had numerous discussions on evaluation, some of which have been ongoing for the past ten years.

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We would also like to acknowledge financial support from the Natural Science and Engineering Research Council of Canada.

Many thanks to our first editor at Cambridge University Press, Heather Bergman, whose confidence in our project was very uplifting. She made contract negotiations very easy, with her dynamism and encouragement. Lauren Cowles, who succeeded her as our editor, has been equally competent and helpful. Lauren indeed made the administrative process extremely easy and efficient, allowing us to devote more time to the ideas and contents of the book. Our copy editor Victoria Dahany deserves a special thank you for her meticulous work and the painstaking effort to refine our discussion without which this book would not have been in its present form. We would also like to thank Victoria for her encouraging notes during the copyediting phase that reinforced our belief in both the importance and pertinence of the subject matter. We would also like to thank David Jou, Marielle Poss, Katy Strong, and the Cambridge marketing team for their thorough professionalism and help with processing the book and disseminating the information as well as with design aspects of the marketing material. Also, the team at Aptara, especially Sweetey Singh, Tilak Raj, and Pushpender Rathee, has been thoroughly professional in taking the book publication forward from copyediting to its final version.

Nathalie would also like to thank her husband, Norrin Ripsman, for sharing his experience with writing and publishing books. His advice on dealing with presses and preparing our material was particularly helpful. On a more personal note, she appreciated him for being there every step of the way, especially at times when the goal seemed so far away. Her daughter Shira also deserves great thanks for being the excellent girl that she is and bearing with her Mum's work all along. The baby-to-be, now lovely little Dafna, showed tremendous patience

Cambridge University Press

978-0-521-19600-0 - Evaluating Learning Algorithms: A Classification Perspective

Nathalie Japkowicz and Mohak Shah

Frontmatter

[More information](#)

xiv

Preface

(in both her fetal and infant states), which made it possible for Nathalie to continue working on the project prior to and after her birth. Nathalie's father, Michel Japkowicz, and her mother, Suzanne Japkowicz, have also always been an unconditional source of loving support and understanding. Without their constant interest in her work, she would not be where she is today. Nathalie is also grateful to her in-laws, Toba and Michael Ripsman, for being every bit as supportive as her own parents during the project and beyond.

On the personal front, Mohak would like to acknowledge his mother Raxika Shah and his sister Tamanna Shah for their unconditional love, support, and encouragement. It is indeed the unsung support of family and friends that motivates you and keeps you going, especially in difficult times. Mohak considers himself exceptionally fortunate to have friends like Sushil Keswani and Ruma Paruthi in his life. He is also grateful to Rajeet Nair, Sumit Bakshi, Arvind Solanki, and Shweta (Dhamani) Keswani for their understanding, support, and trust.

Finally, we heartily apologize to friends and colleagues whose names may have been inadvertently missed in our acknowledgments.

Nathalie Japkowicz and Mohak Shah
Ottawa and Montreal
2010

Acronyms

2D	two-dimensional	Inf	infimum
3D	three-dimensional	KDD	Knowledge Discovery in Databases (Archive)
ALL	acute lymphoblastic leukemia	KL	Kullback–Leibler
AML	acute myloid leukemia	KS	Kolmogorov–Smirnov
ANOVA	analysis of variance	LOO	leave-one-out
ARI	adjusted Rand index	MAP	maximum a posteriori
AUC	area under the (ROC) curve	MDS	multidimensional scaling
Bin	Binomial (distribution)	MRI	Magnetic Resonance Imaging
BIR	Bayesian information reward	NEC	normalized expected cost
CD	critical difference	NHST	null hypothesis statistical testing
CDF	cumulative distribution function	NPV	negative predictive value
CTBT	Comprehensive Nuclear Test Ban Treaty	PAC	probably approximately correct
CV	cross-validation	PPV	positive predictive value
DEA	data envelopment analysis	PR	precision-recall
DET	Detection Error Trade-Off	RMSE	root-mean-square error
ERM	empirical risk minimization	ROC	receiver operating characteristic (curve)
exp	exponential	ROCCH	ROC convex hull
HSD	honestly significant difference	ROCR	ROC in R package
IBSR	Internet Brain Segmentation Repository	SAR	metric combining squared error (S), accuracy (A), and ROC area (R)
iff	if and only if	SAUC	scored AUC
i.i.d.	independently and identically distributed	SCM	set covering machine

xvi

Acronyms

SIM	simple and intuitive measure	SVM	support vector machine
SRM	structural risk minimization	UCI	University of California, Irvine
SS	sums of squares	VC	Vapnik–Chervonenkis
		w.r.t.	with regard to

Algorithms

1NN	1-nearest-neighbor	NN	nearest neighbor
ADA	AdaBoost using decision trees	RF	random forest
C45	decision tree (c4.5)	RIP	Ripper
NB	naive Bayes	SCM	set covering machine
		SVM	support vector machine

Algorithms are set in small caps to distinguish them from acronyms.

Acronyms used in tables and math

CI	confidence interval	LR	likelihood ratio
FN	false negative	Pr	probability
FP	false positive	TN	true negative
FPR	false-positive rate	TP	true positive
IR	information reward	TPR	true-positive rate

These are not acronyms, although sometimes TPR and FPR will appear as such. Authors' preferences were followed in this case.