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Edited by Raf Cluckers, Johannes Nicaise, Julien Sebag

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Motivic Integration and its Interactions with Model Theory and Non-Archimedean Geometry

Volume I

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