# **Applied Digital Signal Processing**

Master the basic concepts and methodologies of digital signal processing with this systematic introduction, without the need for an extensive mathematical background. The authors lead the reader through the fundamental mathematical principles underlying the operation of key signal processing techniques, providing simple arguments and cases rather than detailed general proofs. Coverage of practical implementation, discussion of the limitations of particular methods, and plentiful MATLAB illustrations allow readers to better connect theory and practice. A focus on algorithms that are of theoretical importance or useful in real-world applications ensures that students cover material relevant to engineering practice, and equips students and practitioners alike with the basic principles necessary to apply DSP techniques to a variety of applications. Chapters include worked examples, problems, and computer experiments, helping students to absorb the material they have just read. Lecture slides for all figures and solutions to the numerous problems are available to instructors.

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# Applied Digital Signal Processing

# THEORY AND PRACTICE

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> To my wife and best friend Anna and in memory of Eugenia, Gregory, and Elias DGM

To my loving wife Usha and daughters Natasha and Trupti for their endless support. VKI

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# PREFACE

During the last three decades Digital Signal Processing (DSP) has evolved into a core area of study in electrical and computer engineering. Today, DSP provides the methodology and algorithms for the solution of a continuously growing number of practical problems in scientific, engineering, and multimedia applications.

Despite the existence of a number of excellent textbooks focusing either on the theory of DSP or on the application of DSP algorithms using interactive software packages, we feel there is a strong need for a book bridging the two approaches by combining the best of both worlds. This was our motivation for writing this book, that is, to help students and practicing engineers understand the fundamental mathematical principles underlying the operation of a DSP method, appreciate its practical limitations, and grasp, with sufficient details, its practical implementation.

# **Objectives**

The principal objective of this book is to provide a systematic introduction to the basic concepts and methodologies for digital signal processing, based whenever possible on fundamental principles. A secondary objective is to develop a foundation that can be used by students, researchers, and practicing engineers as the basis for further study and research in this field. To achieve these objectives, we have focused on material that is fundamental and where the scope of application is not limited to the solution of specialized problems, that is, material that has a broad scope of application. Our aim is to help the student develop sufficient intuition as to how a DSP technique works, be able to apply the technique, and be capable of interpreting the results of the application. We believe this approach will also help students to become intelligent users of DSP techniques and good critics of DSP techniques performed by others.

# **Pedagogical philosophy**

Our experience in teaching undergraduate and graduate courses in digital signal processing has reaffirmed the belief that the ideal blend of simplified mathematical analysis and computer-based reasoning and simulations enhances both the teaching and the learning of digital signal processing. To achieve these objectives, we have used mathematics to support underlying intuition rather than as a substitute for it, and we have emphasized practicality without turning the book into a simplistic "cookbook." The purpose of MATLAB<sup>®</sup> code integrated with the text is to illustrate the implementation of core signal processing algorithms; therefore, we use standard language commands and functions that have remained relatively stable during the most recent releases. We also believe that in-depth

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#### Preface

understanding and full appreciation of DSP is not possible without familiarity with the fundamentals of continuous-time signals and systems. To help the reader grasp the full potential of DSP theory and its application to practical problems, which primarily involve continuous-time signals, we have integrated relevant continuous-time background into the text. This material can be quickly reviewed or skipped by readers already exposed to the theory of continuous-time signals and systems. Another advantage of this approach is that some concepts are easier to explain and analyze in continuous-time than in discrete-time or vice versa.

## **Instructional aids**

We have put in a considerable amount of effort to produce instructional aids that enhance both the teaching and learning of DSP. These aids, which constitute an integral part of the textbook, include:

- **Figures** The graphical illustrations in each figure are designed to provide a mental picture of how each method works or to demonstrate the performance of a specific DSP method.
- Examples A large number of examples are provided, many generated by MATLAB<sup>(R)</sup> to reflect realistic cases, which illustrate important concepts and guide the reader to easily implement various methods.
- MATLAB<sup>®</sup> functions and scripts To help the reader apply the various algorithms and models to real-world problems, we provide MATLAB<sup>®</sup> functions for all major algorithms along with examples illustrating their use.
- Learning summaries At the end of each chapter, these provide a review of the basic yet important concepts discussed in that chapter in the form of a bullet point list.
- **Review questions** Conceptual questions are provided at the end of each chapter to reinforce the theory, clarify important concepts, and help relate theory to applications.
- **Terms and concepts** Important phrases and notions introduced in the chapter are again explained in a concise manner for a quick overview.
- **Problems** A large number of problems, ranging from simple applications of theory and computations to more advanced analysis and design tasks, have been developed for each chapter. These problems are organized in up to four sections. The first set of problems termed as Tutorial Problems contains problems whose solutions are available on the website. The next section, Basic Problems, belongs to problems with answers available on the website. The third section, Assessment Problems, contains problems based on topics discussed in the chapter. Finally, the last section, Review Problems, introduces applications, review, or extension problems.
- **Book website** This website will contain additional in-depth material, signal datasets, MATLAB<sup>®</sup> functions, power-point slides with all figures in the book, etc., for those who want to delve intensely into topics. This site will be constantly updated. It will also provide tutorials that support readers who need a review of background material.
- Solutions manual This manual, which contains solutions for all problems in the text, is available to instructors from the publisher.

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# Audience and prerequisites

The book is primarily aimed as a textbook for upper-level undergraduate and for first-year graduate students in electrical and computer engineering. However, researchers, engineers, and industry practitioners can use the book to learn how to analyze or process data for scientific or engineering applications. The mathematical complexity has been kept at a level suitable for seniors and first-year graduate students in almost any technical discipline. More specifically, the reader should have a background in calculus, complex numbers and variables, and the basics of linear algebra (vectors, matrices, and their manipulation).

# **Course configurations**

The material covered in this text is intended for teaching to upper-level undergraduate or first-year graduate students. However, it can be used flexibly for the preparation of a number of courses. The first six chapters can be used in a junior level signals and systems course with emphasis on discrete-time. The first 11 chapters can be used in a typical one-semester undergraduate or graduate DSP course in which the first six chapters are reviewed and the remaining five chapters are emphasized. Finally, an advanced graduate level course on modern signal processing can be taught by combining some appropriate material from the first 11 chapters and emphasizing the last four chapters. The pedagogical coverage of the material also lends itself to a well-rounded graduate level course in DSP by choosing selected topics from all chapters.

## Feedback

Experience has taught us that errors – typos or just plain mistakes – are an inescapable byproduct of any textbook writing endeavor. We apologize in advance for any errors you may find and we urge you to bring them or additional feedback to our attention at vingle@ece.neu.edu

## **Acknowledgments**

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> Dimitris G. Manolakis Vinay K. Ingle